

Doctoral School in Materials Science and Engineering

Engineered Alumina / Silicon Carbide Laminated Composites

Francesca De Genua



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ENGINEERED ALUMINA/SILICON CARBIDE LAMINATED COMPOSITES

Francesca De Genua

E-mail: francesca.degenua@ing.unitn.it

Approved by:

Prof. V.M. Sglavo, Advisor Department of Industrial Engineering University of Trento, Italy.

Ph.D. Commission:

Prof. G. Straffelini, Department of Industrial Engineering University of Trento, Italy.

Prof. M. R. Chierotti, Department of Chemistry University of Torino, Italy.

Prof. P. Fermo, Department of Inorganic, Metallorganic and Analytic Chemistry *University of Milano, Italy.*

Prof. M. Scoponi, ISOF Institute *CNR of Bologna, Italy.*

University of Trento,

Department of Industrial Engineering

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Francesca De Genua - 2014 Published in Trento (Italy) – by University of Trento ISBN: To my daughter Chiara, desidera e tenta, perché di aspirazioni e tentativi è fatta la vita.

Abstract

High-melting temperature oxides, carbides and nitrides are superior in hardness and strength to metals, especially in severe conditions. However, the extensive use of such ceramics in structural engineering applications often encountered critical problems due to their lack of damage tolerance and to the limited mechanical reliability. Several ceramic composites and, in particular, laminated structures have been developed in recent years to enhance strength, toughness and to improve flaw tolerance. Significant strength increase and improved mechanical reliability, in terms of Weibull modulus or minimum threshold failure stress, can be achieved by the engineering of the critical surface region in the ceramic component. Such effect can be realized by using a laminated composite structure with tailored sub-surface insertion of layers with different composition. Such laminate is able to develop, upon co-sintering, a spatial variation of residual stress with maximum compression at specific depth from the surface due to the differences in thermal expansion coefficient of the constituting layers.

In the present work silicon carbide has been selected as second phase to graduate the thermal expansion coefficient of alumina due to its relatively low specific density that could allow the production of lighter components with improved mechanical performance, also for high temperature applications. Ceramic laminates with strong interfaces composed of Al₂O₃/SiC composite layers were produced by pressureless sintering or Spark Plasma Sintering (SPS) of green layers stacks prepared by tape casting water-based suspensions. Monolithic composites containing up to 30 vol% silicon carbide were fabricated and thoroughly characterized. Five engineered ceramic laminates with peculiar layers combination that is able to promote the stable growth of surface defects before final failure were also designed and produced. By changing the composition of the stacked laminae and the architecture of the laminate, tailored residual stress profile and T-curve were generated after co-sintering and successive cooling in each multilayer.

The results of the mechanical characterization show that the engineered laminates are sensibly stronger than parent monolithic composite ceramic and exhibit surface damage insensitivity, according to the design. Such shielding effect is especially observed when macroscopic cracks are introduced by high load Vickers indentations. Some designed multilayers exhibit reduced strength scatter and higher Weibull modulus, which implies superior mechanical reliability. Fractographic observations on fracture surfaces of the engineered laminates show a graceful crack propagation within the surface layers in residual compressive stress which can be attributed to the stable growth of superficial cracks before final failure as it is predicted by the apparent fracture toughness curve. Such fracture behaviour is considered to be responsible for the peculiar surface damage insensitivity and the improved mechanical performance.

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Chapter I

Introduction

Materials have always been an integral part of human culture and civilization. The role of materials has been so important that historians have identified early cultures by the most significant material used then, consider the Stone, the Bronze and the Iron Ages of the past. Today, we are not limited to one predominant material. Engineers adapt materials to society's needs and advanced technologies rely on sophisticated materials thus we can refer to our modern society as the "age of technology" [1].

Ceramics industry is the largest raw materials industry and ceramics are encountered in virtually every facet of everyday life. Traditional ceramics such as cements, glasses, refractories and clays are largely silica or clay based and typically involve low-cost fabrication processes. The main use of these ceramics is focused on tableware, sanitary wares, fireclays, construction materials and applications involving static loading in compressive locations. This use exploits the dominating characteristics of ceramics as chemical stability, high melting point, high hardness, high elastic modulus and compressive strength, and higher resistance than that of either metals or polymers to high temperatures and to severe environments [1–3]. In view of such an attractive combination of properties, the development and discovery of novel uses of ceramic materials have been improved and ceramics have been considered as potential materials for many sectors of industrial society as aerospace, electronics, nuclear, biomedical, catalytic, electronic, communication, structural and tribological applications [4].

Adequate mechanical properties as strength, hardness, toughness and wear resistance are of prime importance for structural applications. An optimum combination of high toughness with high hardness and strength is usually required. Therefore, in the past decades, the study of mechanical behaviour of ceramics and the development of ceramic materials with proper combination of mechanical properties has been the major focus in the ceramics community [5]. This has led to

the discovery of new classes of structural ceramic materials that are typically used in components which are load bearing and at the same time exposed to severe conditions of wear, corrosion and temperature. Significant success has been achieved in many modern designs as cutting-tool technologies, wear resistant components, heat exchangers, prosthetics, heat engine components, thermal barrier coatings and ballistic armour [4].

Unfortunately, ceramics are inherently strong in compression but apparently week in tension and bending. General attributes seriously affecting an extensive application of ceramics as structural materials are their lack of the requisite toughness, brittleness and variability in strength. The strength of ceramics is indeed statistical by nature of the flaw distribution within the body because any geometric irregularity leads to a stress concentration. The average size, size distribution and type of inhomogeneity determines average strength and strength distribution. Moreover a crack once started may grow spontaneously when the critical stress intensity is exceeded and, without ample ductility, no energy is consumed by plastic deformation. Therefore, the failure is brittle, immediate and occurs in catastrophic manner while the wide strength scatter lead to poor mechanical reliability and impair safe design [6–8].

In order to overcome these problems, two principal routes have been explored in the last decades and the challenge for scientists has been to make ceramics stronger or tougher. The first route consists in decreasing flaw presence and severity with more sophisticated preparation process control, proof testing or by reducing the component dimensions [9,10]. Glass fibres are a typical example used to show that, if no flaws are present, the tensile strength will be as high as the compressive strength. If protected from surface abrasion, glass fibres attain strengths greater than steel [8]. The ceramics community has been involved with more interest in the second route that regards the design and development of new materials and structures with increasing toughness and improved flaw tolerance [6,8]. In this case, fracture is controlled by a toughness curve and the material possesses a T-curve behaviour. Current approaches to toughening are energy dissipative and increase the apparent strain before fracture is completed. Since plastic deformation is strongly inhibited in ceramics, this process can involve several microstructural toughening mechanisms as matrix microcracking, fibre debonding and phase transformation toughening. In the first two mechanisms, fractured surfaces are increased markedly so more surface energy has to be provided, micro-displacements appear as apparent strains and the energy consumption during fracture is increased. Polycrystalline structures with anisotropic grains or composite structures with particles, platelets, whiskers or fibers as second phases were produced to exhibit crack pinning, crack crack bridging, fibre pullout, deflection. debonding and stress-induced microcracking [11,12]. Phase transformation toughening utilizes a rapid stress induced structural transformation that involves a molar volume increase and/or shape change. The increased toughness is derived from the work required to induce the transformation in the vicinity of the propagating crack and from the compressive stresses produced by volume expansion that strengthen the material ahead of the crack tip. This concept has been applied in monolithic zirconia and systems containing dispersed zirconia particles [11,12]. Stress induced plasticity in metallic binder and dispersed phases also enhanced fracture resistance [8]. Unfortunately, all these solutions require an accurate control of raw materials and processing, are quite expensive and only partially overcome the problem of strength scatter.

The latest developments in ceramic composites show that the use of layered structures is the most promising method to increase mechanical performances and reliability. Indeed, with multilayer ceramics it is possible to design a structure that can be used to control cracks and brittle fracture. Some metal/ceramic laminates and several multilayer ceramics, produce in a wide range of materials as alumina, zirconia, silicon carbide, silicon nitride and boron nitride, have been investigated in the past. In metal/ceramic laminates, the toughness enhancement is controlled by the closure exerted by the metallic bridging layers astride the crack [13]. In ceramic laminates, toughness has been enhanced by the introduction of weak interfaces or internal stresses. The presence of weak interfaces allows for energy dissipation before fracture through mechanisms of crack deflection, crack bridging and interface delamination. The weakness is given by layers not wholly sintered, generally a different material with respect to the main multilayer component, or by the addition of pore forming agents in specific layers, bringing to porous structures [14–16]. Although the improvements in fracture resistance in these laminates were sufficient

to ensure their safe use in many structural applications, delamination and easy crack propagation along the weak interface has been the major impediment for a wider use. In the case of ceramic laminates with strong interfaces, strength and toughness has been enhanced through design of controlled residual stresses. Tempered glasses are a well recognize and inexpensive method to enhance mechanical properties by the introduction of surface compressive stresses [1]. This goal can be achieved in ceramics through the production of laminates where residual stresses arise from differences in sintering rates. Young's modulus or thermal expansion coefficients among the laminae of dissimilar materials. The layer composition, as well as the system's geometry, allows the designer to control the magnitude of the residual stresses. In particular, if compressive stresses are located at the surface of the multilayer, strength is enhanced [17]. Reliability is favoured when compressive residual stresses are induced in internal layers as in laminated structures composed of alternating thin compressive layers and thicker tensile layers. These laminates are characterized by a threshold strength below which rupture does not occur [18,19]. The most important limitation of such multilayers is that they can be used only with specific orientations to the applied load and they are not suitable for producing shells or tubes usually required in industrial applications.

Recently, Sglavo and co-workers [20–25] have demonstrated that the introduction of a residual stress profile with the maximum compression at a certain depth from the surface of a glass or a ceramic laminate can force the stable propagation of surface flaws up to this specific depth before the final catastrophic failure. Therefore, these materials exhibit high strength independent on the dimensions of inherent defects and characterized by a limited scatter. High mechanical reliability or minimum strength have been experimentally observed in oxides laminated structures. In addition, the production of these innovative ceramic laminates is economic because based on common ceramic materials and inexpensive conventional fabrication methods. These laminated bodies are therefore natural candidates for structural applications as in the case of load bearing components in automotive and aircraft industry, biomedical prosthesis, chemical plant linings and safety systems. The motivation for the use of these laminated composites can be traced back to the observation of biological structures in which the most performing

parts of the material are located in regions that experience the highest stresses.

In this work, the approach proposed by Sglavo has been followed to design and develop new alumina/silicon carbide composite laminates with high thermomechanical performances. This materials system has been selected to produce lower density bodies respect to the oxides systems previously studied. In fact, more often density becomes a limitation or a requirement in selecting the ceramics for structural, defence and biomedical applications. In addition, alumina and silicon carbide possess higher thermal conductivity than most other ceramics. Thus they are less subject to thermal cracking from sharp temperature gradients and have potential for dynamic high temperature service such as rotors in gas turbines [1]. Alumina/silicon carbide composites have been studied extensively for their good thermo-mechanical behaviour, especially remarkable high-temperature creep resistance, and alumina itself is a potential matrix for structural composites with high temperature capability because of its good stability at high temperatures [11]. The alumina/silicon carbide system represents also a challenge because of the adverse effects during sintering, as weight loss and poor densification, so they are generally prepared by hot pressing [11,26].

In the present paper, alumina/silicon carbide multilayered ceramics with residual stress profiles engineered to promote the propagation of surface defects in a stable manner up to a maximum depth have been designed and produced by tape casting, lamination and sintering. Specifically, pressureless sintering and Spark Plasma Sintering have been used for novel laminates manufacturing routes. The results of the mechanical characterisation of the engineered laminates, compared to the behaviour of simple homogeneous laminates, prove that the manufacturing procedure described in this work can be used successfully to produce alumina/silicon carbide composite laminates with improved reliability. Evidences of stable growth phenomena occurring in the laminates have been demonstrated by the analysis of the post indentation strength and by fractographic analysis.

Chapter II

Background

2.1 Fracture behaviour of ceramic materials

2.1.1 Brittle behaviour and strength scatter

Ceramics are compounds that contain metallic and non metallic elements held together by very strong covalent or ionic partially covalent bonding. Considerable energy is required to break these bonding, therefore ceramic materials exhibit refractoriness, chemical inertia, high elastic modulus and hardness, also at temperatures above 1000°C. The chemical structure of this class of materials is also responsible of another typical feature of ceramics: brittleness. The strong atomic bonding do not allow a relevant plastic deformation, in which sliding between crystalline planes occurs, and fracture happens essentially by bond rupture that propagates in the body at high velocity and low stress levels in elastic field. Therefore fracture occurs in brittle and catastrophic manner. Little energy is absorbed in brittle fracture, just the energy to separate atoms and create new surface is required. Negligible energy for plastic deformation or other dissipative processes is involved over most of their useful range of operational temperature. As a consequence, the energy requirement to fracture, or fracture toughness, of ceramics is poor, with values typically below 5 MPa m^{0.5} [5,6].

Linear Elastic Fracture Mechanics (LEFM) is the basic theory of fracture that deals with sharp cracks in elastic bodies. It is generally applied to materials that exhibit linear elastic behaviour up to failure, as ceramics [7,8]. The basis of LEFM has been originally developed by Griffith (1920) in realizing that bulk strength of most materials is lower than the theoretical cohesive strength predicted from interatomic potential considerations. He assumed most materials must contain cracks that act as stress concentrators and reduce the maximum load bearing capability. Griffith considered an infinite plate of unit thickness subjected to an external

uniform tensile loading and containing a through-thickness crack. He suggested a criteria for the crack extension by developing an energy approach in which the static crack is considered as a thermodynamically reversible system and fracture is a process controlled by energy exchanges between the body and the loading system. In 1948 Irwin observed that the energy balance proposed by Griffith involves terms promoting crack extension and a term representing the resistance of the material. So he defined two parameters: the "strain energy release rate" G as fracture driving force and the "crack resistance force" R that represents all the crack propagation resistance processes available inside the material. In addition, Irwin suggested that all stress systems in the vicinity of a crack can be derived by only three modes of loading of the crack faces (crack opening mode or mode I, shear mode or mode II and tearing mode or mode III) and demonstrated, using an elastic analysis of stresses, that the local tensions near a crack are higher than the stress applied to the body. This amplification of stresses near the crack tip is represented by a parameter called "stress intensity factor" K. Irwin proposed a simple relationship between K and G and introduced a stress approach alternative to the energy approach. Both approaches compare the moving force for crack propagation and the relative material resistance pointing out that fracture occurs when a critical condition is reached. In particular, failure is considered to occur when G and K, functions of stress state and crack geometry, reach respectively R and the "fracture toughness" K_c. These critical values are material intrinsic properties.

In this work, the stress approach and, for synthesis, only the crack loading mode I will be considered. Among the three crack loading modes, mode I is indeed the more common and dangerous in brittle materials. The stress intensity factor K_I corresponding to mode I is expressed by the relationship:

$$K_{I} = Y\sigma(\pi c)^{0.5} \qquad \qquad Eq. (2.1)$$

where Y is a dimensionless parameter that depends on the crack and loading geometries, σ is the nominal applied stress and c is the crack length as measured along the direction normal to the stress axis. The equilibrium condition for the crack propagation is reached when K_I reaches the critical value K_{IC}:

Therefore, only the material toughness K_{IC} and the defect dimension c are necessary to completely describe the material strength σ_b as in the equation:

$$\sigma_{\rm b} = \frac{K_{\rm IC}}{Y(\pi c)^{0.5}} \qquad \qquad Eq. (2.3)$$

Considering Eq. (2.1) and Eq. (2.3) it is possible to represent the applied stress as the angular coefficient of a straight line through the origin in the graphic $K_I/(Y\pi^{0.5})$ vs c^{0.5} (Figure 2.1). So, the strength of a material of toughness K_{IC} , independent of crack length, can be easily identified when the defect dimension is known.



Figure 2.1: Strength as a function of single-value fracture toughness K_{IC} and defect dimension c in the graphic $K_{I}/(Y\pi^{0.5})$ vs $c^{0.5}$. Strengths σ_{b0} and σ_{b1} relatives to c_0 and c_1 crack lengths are shown.

Defects considered in Fracture Mechanics are sharp cracks with a well defined geometry. In brittle materials these defects are generally assumed to form by cleavage of atomic bonds in regions in which there are high local stresses. These high stresses arise because of the heterogeneous nature of the material at the microstructural level or because of inelastic deformation that cannot be accommodated [6]. Defects, generally present both inside the component and on its surface, can form during processing from voids, inclusions or agglomerates or can produced during subsequent service from thermal shock or contacts events as impacts, erosion and wear. Surface defects are considered more severe for ceramics because bending load is usually applied and because internal flaws are more easily avoidable through processing optimization. These crack like defects form a variable and unknown statistic population, usually of the order of 5 μ m to 200 μ m in size [27], that according to Eq. (2.3) lead to a strength distribution. Brittle fracture strength depend on the stressed volume or surface area and typically exhibit significant scatter, frequently with a coefficient of variation about the mean in excess of 10% [27]. Consequently, ceramics are not characterized by a fracture strength with a limited variability, useable safely in design, and manifest a poor mechanical reliability that restrict their use in structural applications.

A probabilistic prediction of material performance is widely adopted for materials which strength depends on the presence of an unknown defects population. This variability in strength is often express in terms of probability of failure Pf of a sample under a stress or probability of survival $P_s = 1 - P_f$. These probability, related to the probability of existence in the material of defects of specific dimensions, are generally calculated by using the probabilistic model developed by Weibull and based on the weakest link fracture theory. The Weibull distribution of flaws is usually adopted as statistical approach due to its capability to analyze material's phenomena represented by a symmetrical and asymmetrical data set. In the weakest link approach the probability of occurrence of two events is the product of the probability that each event take place independently. The test sample is considered as a chain made of N elements and the failure of the entire chain happens when the rupture of the weakest link befall. According to this approach, fracture is controlled by the most critical defect, that is the defect of largest dimension favourably oriented toward the tensile stress direction. The Weibull failure probability at a given stress σ is defined in its simplest form by the two empirical parameters relation:

where σ_0 is the characteristic strength and m is the Weibull modulus. The characteristic strength can be interpreted as the strength value in which the cumulative probability of failure of a body with unit volume is 63.2% and can be calculated setting $\sigma = \sigma_0$ in Eq. (2.4). It is related to the mean strength and dislocates the distribution of strength in the stress space. The Weibull modulus describes the scattering of the mechanical strength data. For ceramics, m is usually of the order of 5 to 20 [6], in particular of about 10 [8] for conventional as-finished ceramics while, for structural ceramics, m varies between 3 and 12 [28], depending on processing conditions. The higher the m value, the lower is the strength dispersion and the higher the mechanical reliability. The expression of Eq. (2.4) is usually rearranged in terms of logarithms to obtain the following relationship which allows an easy estimation of the Weibull parameters:

$$\ln\left[\ln\left(\frac{1}{1-P_{\rm f}}\right)\right] = m\ln\sigma - m\ln\sigma_0 \qquad \qquad Eq. (2.5)$$

Indeed, in the diagram $\ln[\ln(1/1-P_f))]$ vs. In σ (Figure 2.2) the Weibull modulus can be calculated from the slope of the straight line of the distribution function and the characteristic strength from the intercept with the tension axis. The fitting of a straight line is often done using linear regression. In such a procedure, the total number of failure strength data N have to be arrange in ascending order and the probability of failure P_fⁱ of the sample with rank i have to be estimate as:

$$P_{f}^{i} = \frac{i - 0.5}{N}$$
 (i = 1....N) Eq. (2.6)

Fracture tests have to be performed on a statistically significant number of samples, usually between 30 and 50, to know the Weibull parameters with any accuracy [6]. The Weibull analysis is valid for an isotropic material containing a uniform

distribution of isolated, not interacting defects and undergoing to fracture for unstable propagation of the largest defect.



Figure 2.2: Weibull diagram for soda-lime glass and a vitreous-bonded polycrystalline alumina tested under inert conditions [8].

Several alternatives have been proposed to overcome the problem of an unacceptably high failure probability for typical design stress. One approach is to reduce the strength dispersion and to improve the mechanical reliability of single value toughness materials without changing the fracture toughness. This could be accomplished by reducing the presence and/or dangerousness of defects by shrinking the flaws distribution and limiting the largest defect dimension. For this aim, some sophisticated powder processing technologies [10], that abate the density and dimension of defects, and methods as crack healing [9], applicable to ceramics that have the ability to heal cracks and recover strength, have been developed. Proof testing [6,8] is also used, especially in aerospace and aircraft field, as a technique to control the strength distribution. In a typical proof test, components are subjected to a proof stress higher than that anticipated in service in severe conditions. The weak components, with the largest flaws, fail or give an indication of failure and are discarded. The survivor components exhibit a threshold stress, a minimum value of stress under which the failure probability is zero (Figure 2.3). Thus, proof testing truncates the strength distribution at lower stresses, guarantees that all components will be at least as strong as the proof stress and establish a well defined stress level for design. This method is very expensive, generates a high amount of waste products and cannot be easily performed on big components. In addition, only the severity of processing defects can be reduced while the reliability decrease due to defects generated during service can not be avoided. Potential problems occur also when subcritical crack growth accompanies proof testing.



Figure 2.3: Weibull plots for hot-pressed silicon nitride before (open circles) and after (filled circles) proof testing at $\sigma = \sigma_P$ [8].

2.1.2 T-curve behaviour and microstructural toughening

In the early use of fracture mechanics, brittle ceramics was considered to assume a fracture toughness independent on crack length [6]. In this case, the equilibrium condition for crack propagation is defined by Eq. (2.2). Now, consider a body with single value toughness K_{IC} containing a crack of length c_0 and subjected to an applied load gradually increased from zero to a maximum level (Figure 2.1). At low stress levels the corresponding stress intensity factor K_I is lower than K_{IC} and the crack maintains its length, if subcritical phenomena are not active. When the applied stress is high enough to reach the critical conditions expressed by Eq. (2.2), and thus the σ_{b0} value, the crack initiate to propagate. Moreover, as the crack

extends, the applied stress intensity factor increases more rapidly then the material toughness, a finite difference between K_I and K_{IC} is produced and the excess energy stored in the material is dissipated in kinetic energy as crack acceleration. The crack begins its acceleration on a relatively smooth surface or "mirror zone" [8]. The running crack speed increases up to a maximum value related to the motion ability of the local stress field near the crack tip. When the maximum speed is reached, the mechanical energy released by crack propagation is dissipated in branching and noising. At this critical stage of propagation severe surface roughening or "hackle zone" is produced. An intervening transition region of fine scale subsidiary fracturing of "mist zone" is also present (Figure 2.4). This kind of fracture propagation is unstable.



Figure 2.4: Fracture surface of fused silica glass rod broken in bending, showing mirror, mist and hackle zones spreading outward from fracture origin (indicated by the arrow in the lower edge) [29].

However stable, slow and quasi-static, crack growth is also possible in two particular circumstances. In some cases the combination of sample geometry and loading conditions can lead the applied stress intensity factor to decrease with increasing crack length. This requirement is satisfied for fixed grip loading conditions on a material exhibiting single value toughness as in the Obreimoff (1930) experiment on the cleavage of mica [6,8]. For this case, the crack propagates to an equilibrium length but immediately arrest, since the stress intensity factor is lower than the toughness for any further crack increment. To restart propagation it is necessary to increase the displacement. The second circumstance occurs in materials exhibiting a fracture toughness that increases steeper than the applied stress intensity factor with crack extension. These materials experience the T-curve behaviour, where T means toughness. When the energy approach is followed, the denomination R-curve behaviour, where R is the resistance to crack growth, is commonly used. Therefore, the conditions of stable propagation of crack are satisfied when the equilibrium is satisfied and when the increase of toughness with crack extension is larger than the corresponding increase of stress intensity factor:

The crack growth behaviour can be more complex depending on the variability of the fracture toughness with crack length and hence on the trend that the T-curve assumes in the graphic $K_1/(Y\pi^{0.5})$ vs c^{0.5}. Consider a body, that exhibit a generic T-curve as in Figure 2.5, subjected to a load progressively increased from zero. When the stress level σ_1 is reached, stable propagation of cracks of length c_1 starts, since no energy excess is available for crack acceleration. All the defects of dimension included in the finite interval $[c_1, c_2]$ also propagate in a stable manner. They are equally critical and lead to failure at the same stress level σ_2 . If the inherent defect population is included in such interval, a single value strength is observed. When the body contains flaws of dimensions shorter than the stability interval, unstable fracture occurs. Cracks with dimensions included between c_0 and c_1 propagate in unstable fashion for stresses between σ_1 and σ_2 . Due to their acceleration such cracks can growth up to a length greater than c_2 leading to fracture for stresses lower than σ_2 and scattered.



Figure 2.5: T-curve with a stable crack growth interval $[c_1,c_2]$. Straight lines correspond to the applied stress intensity factor associated to the threshold stress σ_1 and the strength σ_2 .

Fracture toughness, considered as a function of crack length, is more properly a function of the crack length increase in materials where toughening processes at the crack tip are active on growing cracks. The T-curve behaviour of such materials is a key factor to obtain a reduced defect sensitivity, or flaw tolerance, a lower strength scatter, a better mechanical reliability and a more wide industrial application. For this reason, fracture mechanics concepts have been used by scientists to study toughening mechanisms and to produce new ceramics with manipulated microstructure and improved mechanical behaviour. Plastic deformation mechanisms are inhibited in ceramic materials, thus researchers have developed specific polycrystalline or composites microstructures in which energy dissipative toughening mechanisms are promoted. One theory on how the material microstructure influences crack propagation and toughness is crucial for the study and development of tough ceramics. Unfortunately, the general behaviour of real cracks in ceramic microstructures is too much complex to be treated and several theories, that simplify the model considering a single toughening mechanism at a time, have been proposed. As a matter of fact, different mechanisms can act together

and the total effect is not necessarily a simple linear combination of the single effects. The toughening mechanisms observed in ceramic materials [6–8] can be classified into two principal groups: mechanisms acting with crack tip interaction and mechanisms acting with crack tip shielding. (Table 2.1).

Crack tip interaction		Crack front bowing Crack deflection
Crack tip shielding	Process zone activities	Dislocation clouds Microcracking Phase transformation Ductile second phase
	Crack bridging	Grain bridging Fibrous second phase Ductile second phase

Table 2.1: Toughening mechanisms in ceramic materials

Crack tip interaction occurs when tough obstacle are placed in the material to directly interact with the crack tip and to disturb the crack motion. The obstacle could be second phase particles, fibres, whiskers or regions that are simply difficult to cleave. The toughening effect, related to the characteristics of heterogeneities and to the nature of the interaction between the defect and the reinforcement, is the result of the reduced stress intensification at the crack tip, due to the crack path deviation. The crack has allowed two different mechanisms to avoid the obstacle: crack front bowing or crack deflection.

Crack bowing could be observed when a dispersed tough particle is considered to be crossed by the crack front. The first consequence is a pinning action occurring on the front in the crack plane localised in correspondence of the particle. The crack front locally bends and develops a curvature in order to end normally against the particle (Figure 2.6 (a)). When such a curvature reaches a critical value, the crack overcome the particle. In addition, if the obstacles remain intact, bridging produces an increase in fracture toughness. This mechanism has a limited importance for ceramics because in the most cases the dispersed particles are brittle and break before the bowing effect completes.



Figure 2.6: Crack tip interaction: (a) crack bowing; (b) crack deflection. Direction of crack motion is shown by arrows. (Adapted from [6]).

Crack deflection occurs when the crack is deflected out of the plane that is normal to the applied uniaxial tensile stress (Figure 2.6 (b)). The crack is no longer loaded in a simple mode I and the applied stress intensity factor acting on the crack tip is reduced. Two kind of deflection of crack plane could be observed during propagation: tilting of the crack about an axis parallel to the crack front and twisting about an axis normal to the crack front. A tortuous crack path, manifested as roughness of the final fracture surface, is produced accordingly. This mechanism is present in homogeneous polycrystalline microstructures with week grain boundaries or with residual stresses due to anisotropic grains. In composites, the toughening effect is more important and depends mainly on the volume fraction and distribution of the second phase and on the geometry and aspect ratio of the particle. Indeed, toughening by crack deflection is estimated to increase as the obstacle shapes change from spheres, disks and rods. Bridging of grains or second phases could also happen after cracking leading to an improve of the efficacy in toughening. Crack deflection is a dominant toughening mechanisms in alumina reinforced with silicon carbide platelets [6].

Toughening mechanisms acting as crack tip shielding help to protect the material from failures as a shield, reducing the stress intensity near to the propagating crack tip. They are always characterized by a process zone around the crack tip or by a bridging zone behind the crack tip that contains unbroken reinforcing items behaving as ligament between the opposite cracked surfaces. In some cases, process zone and bridging zone could be present together with a synergic effect on fracture toughness. The resistance to crack propagation in the process zone toughening mechanisms is due to phenomena, localised in a circular region in the front of the crack, involving a non linear deformation that reduce the stresses acting on the crack tip. The shielding effect in this region rises from the interaction between the highly intensified stress field and the material heterogeneities. The main process zone toughening mechanisms are dislocation clouds, microcracking, phase transformation and ductile second phase.



Figure 2.7: Process zone toughening mechanisms. (a) dislocation clouds, (b) microcracking, (c) phase transformation and (d) ductile second phase. (Adapted from [8]).

Though the formation of new dislocations in covalent or ionic crystal is thermodynamically hindered, the rearrangement of pre-existent line defects by shear in the highly stressed zone around the crack tip is a possible event (Figure 2.7 (a)). This sort of dislocation recovery requires energy to be performed and produces a slight increase in fracture toughness. Therefore, this mechanism is of limited importance in ceramic materials.

Microcracking phenomenon regards the nucleation and the development of microcracks within the process zone because of the high stress level present in the location (Figure 2.7 (b)). Nucleation starts in intrinsic week sites as intergranular defects or zones containing localized residual tensile stresses. These residual stresses could be the result of phase transformations, thermal expansion anisotropy in single phase polycrystalline ceramics and thermal expansion or elastic mismatch in composite materials. So, microcracking can form spontaneously during fabrication processes, as in a cooling step, due to differences in the thermal expansion coefficient of phases or anisotropic grains. The toughening effect derives from the stress relaxation within the process zone and from the energy dissipated as mechanical work to increase the length and the crack open displacement of microcracks.

Phase transformation toughening is the most important process zone toughening mechanism. This phenomenon could be exploited in materials containing grains able to withstand a phase transformation with volume expansion under the action of the stress field around the propagating crack (Figure 2.7 (c)). Transformation toughening almost always involves the use of partially stabilized zirconia particles in a ceramic matrix, as alumina. Zirconia has several polymorphic transformations as it cools, cubic to tetragonal at 2370°C and tetragonal to monoclinic at 1000–1200°C [6]. The latter step is a martensitic type reaction that involves a $\sim 4\%$ volume expansion and a $\sim 7\%$ shear strain [6]. This step is easily avoided during the cooling process after sintering by stabilizing the tetragonal phase at ambient temperature with several agents as yttria, ceria and magnesia. However the phase transition could also occurs by a shear displacement. Therefore, the application of large mechanical stresses to the composite, as during the fracture process near the crack tip, nucleates the tetragonal to monoclinic phase change. The accompanying volume expansion induces compressive stresses that strengthen the material ahead of the crack tip and increase fracture toughness.

The dispersion of ductile particles, typically metals, in a ceramic matrix is another practical way to increase fracture toughness (Figure 2.7 (d)). The high tensile stresses present in the region around the crack tip allow to reach the yielding condition for the ductile phase and hence the energy consumption in plastic deformation. The fracture toughness increase is also related to the subsequent bridging phenomena by ductile particles acting on the crack surfaces.

Crack bridging mechanisms are due to processes occurring before the crack tip, also at high distances. Pulling forces between the cracked surfaces are developed by the interlock of agents acting as bridges that hinder additional crack opening. The mechanical work required to overcome these pulling forces promotes an increase of fracture toughness. The reinforcing agents can be simple grains, fibres, whiskers or ductile particles. Many monophase polycrystalline ceramics with elongated and large grains exhibit grain bridging after intergranular fracture (Figure 2.8).



Figure 2.8: Grain bridging. (Adapted from [8]).

The shape and dimensions of grains and the presence of residual stresses, that support the grains contact after fracture, are the microstructural variables of this mechanism. In particular, two toughening effects happen when the crack propagates on the intergranular path and runs into a grain boundary. Crack deflection phenomenon occurs because the crack plane is tilted on the grain boundary and it is not yet perpendicular to the applied load. Grain bridging follows the fracture with mechanic interlock and friction between grains. The toughness improvement is higher for longer cracks involving more grains and for bigger grain dimensions. Nevertheless, the grain size has to be small enough to obtain good strength values according to the Hall-Petch relationship [12]. The T-curve behaviour induced by this toughening mechanism in polycrystalline alumina is substantial, especially for grains with size of about $10-20 \mu m$ [30]. The prevalent fracture mode in alumina is indeed the intergranular mode, with transgranular fracture partially present in grains

bigger than 15 µm [8].

The arising of a bridging zone during fracture is an efficient toughening mechanism acting in composite microstructures where a second reinforcing phase is added to a matrix. These ceramic composites can be classified, according to the main active phenomenon, as composites reinforced with brittle embodiments and composites reinforced with ductile second phases.



Figure 2.9: Crack bridging in composites. (a) fibrous second phase, (b) ductile second phase. (Adapted from [8]).

The brittle reinforcements, usually whiskers and fibres, are characterized by toughness values comparable with the matrix one and high strength. Therefore, the bridging zone effect (Figure 2.9 (a)) is usually increased by the presence of week interfaces between the matrix and the second phase. Intact bridges and frictionally sliding bridges, or pull-out, are the basic events observable as the crack propagates. When the bridging item is not broken and still bonded to both crack surfaces, part of the tensile stresses are supported as localised pulling forces by elastic deformation of the item intersected by the crack front. Only the reinforcement in the region near the crack are involved in this pulling action since the crack opening displacement is too large at higher distances. Pull-out occur when the reinforcing agent strength is higher than the adhesion between agent and matrix. This phenomenon of frictionally sliding bridges is always preceded by debonding, a phase when the crack deflects and follows a path along the interfaces reinforcement/matrix. Excluding phase transformation, pull-out is the most effective toughening mechanism in ceramics since the amount of involved energy is considerably large. Quite high toughness values can be also reached when ductile particles are added to a ceramic matrix. The

bridging effect is exerted during the elastic elongation of intact particles up to the yielding condition and during the further plastic deformation of bridges arranged in the region near the crack (Figure 2.9 (b)).

As a consequence of these toughening mechanisms, T-curve behaviour, leading to increase of fracture toughness typically from 1-5 MPa m^{0.5} up to even 35 MPa m^{0.5} [6], and improved mechanical reliability can be observed in proper well-designed monophase or composite microstructures.

2.2 Alumina/silicon carbide composites

Alumina is one of the most popular ceramic materials used in structural applications because of its excellent properties such as chemical stability, high melting temperature, strength, hardness and corrosion resistance. Due to its refractory nature, alumina is widely used in thermal liners, thermal barrier installations, high temperature insulating systems, crucibles and heaters. However, similarly to most ceramics, the intrinsic brittleness of monolithic alumina limits its reliability and prevents its wider usage. Therefore, addition of inert second phase, like hard ceramic particulate, platelets and whiskers, to monolithic alumina is an effective way for strengthening and toughening. The second phases control the microstructure, by suppression of grain growth or control of grain morphology, and improve toughness according to the mechanisms presented previously. Some popular examples of ceramic matrix composites include $Al_2O_3/ZrO_{2(p)}$ and $Al_2O_3/SiC_{(w)}$ which are used as wear parts, bioceramics and cutting-tool inserts.

SiC is an ideal candidate for the reinforcement for alumina composites, especially for structural applications at high temperature, due to its wide availability, low cost, low density and excellent thermal properties, such as low thermal expansion coefficient, high thermal conductivity and high melting point. Conversely, SiC has poor sinterability, owing to its strong covalent bonding and low surface-to-grain boundary energy ratio. Alumina, which has high ionic character and low oxygen diffusion coefficient, compensates the poor sinterability of SiC and protect the carbide from oxidation in severe operative conditions [11,12]. Al₂O₃/SiC composites have been studied extensively for their good mechanical behaviour,

especially good high temperature performances. Large differences in the mechanical properties of Al₂O₃/SiC composites could be obtained because of the variations in microstructure and fracture behaviour related to the effect of different SiC reinforcements shapes as whiskers, platelets and particulates.

2.2.1 SiC whiskers-reinforced alumina composites

SiC whiskers have been successfully incorporated into alumina by many researchers to obtain superior mechanical and tribological properties as compared with conventional monolithic alumina, also at temperatures above 1200°C [11,12,31,32]. Al₂O₃/SiC_(w) is one of the most widely studied ceramic composite materials and it is presently being commercially fabricated for wear and mechanical machining applications. Generally, the SiC whisker diameters and aspect ratios are in the range of 0.1 µm to 1 µm and about 10–20, respectively. Mechanical properties such as fracture toughness and fracture strength of alumina remarkably increase with increasing whisker content, that could reach 40 vol%, as shown in Table 2.2 [11,31]. The increase in fracture toughness of these composites has been attributed to crack deflection due to whiskers presence, with some contribution from crack bridging and whisker pull-out occurring in the process zone around the crack front (Figure 2.10). Rising T-curve behaviour with increasing crack extension has also been observed in these composites, as associated to the toughening mechanisms [32]. However, whiskers reinforced composites are relatively expensive materials to produce and there are health concerns related to the asbestos-like geometry of whiskers. Since microstructural homogeneity of whisker reinforced alumina is of primary importance to achieve successful toughening and its lack may be responsible for strength decrease, whisker agglomeration may represent strength limiting flaw. Unfortunately, it is difficult to obtain good dispersion of whiskers within a matrix and whiskers-containing powder compacts are not easy to compact and densify because of formation of constraining networks of whiskers. These networks usually exert tensional stresses on the matrix and severely inhibit particle rearrangement and shrinkage during sintering. Therefore hot pressing, which leads to composites with anisotropic properties, is a common practice for the densification of whisker containing composites.
Whiskers content [vol%]	Strength [MPa]	Toughness [MPa m ^{0.5}]
0	150	4.3
5	475	4.0
10	540	4.8
15	652	4.6
20	675	6.1
30	641	8.7
40	850	6.2

Table 2.2: Fracture strength and toughness at ambient temperature of $Al_2O_3/SiC_{(w)}$ composites with different whiskers content (Adapted from [11]).



Figure 2.10: SEM micrograph showing the crack propagation in a Al₂O₃/SiC_(w) composite. (Adapted from [11]).

2.2.2 SiC platelets-reinforced alumina composites

The great advantage in using platelets as reinforcements in composite fabrication (Figure 2.11) is related to their less critical geometry respect to whiskers. Platelets are not dangerous to health as are whiskers, are cheaper to manufacture and process, since no special processing technique are required, and could be introduced in a ceramic matrix in higher contents respect to whiskers without agglomeration problems that could hinder densification [11,12,33,34]. Platelets are available in wide range of dimensions and chemical composition. Strength and toughness of alumina can be increased upon the addition of SiC platelets, with careful control of the reinforcements sizes and orientation, but the toughening effect is limited as compared to whiskers reinforced alumina. For example, a toughness value of 7.1 MPa m^{0.5}, with 70% of increase respect to pure alumina, was reported for an alumina composite containing 30 vol% SiC platelets [33]. Crack deflection and grain bridging, acting only when the platelet faces are oriented parallel to the tensile stress direction, are toughening mechanisms leading to the T-curve behaviour.



Figure 2.11: Cross sectional view of hot-pressed Al₂O₃/SiC_(pl) composite [33]. The hot pressing direction was vertical.

2.2.3 SiC particles-reinforced alumina composites

The improvement of the mechanical properties of alumina ceramics by SiC particles as inert second phases is another promising alternative for the more common whisker reinforcement. Effectively, Al₂O₃/SiC particle composites were developed more recently and, in particular, Al₂O₃/SiC nanocomposites have been researched intensively because they have been reported to have drastically improved mechanical properties over the basic alumina [26,35–42].

Nanocomposite materials can be defined as composites of more than one Gibbsian solid phase where at least one of the phases shows dimensions in the nanometre range [26]. The solid phases can be exist either in amorphous, semicrystalline or crystalline states. Niihara and co-workers [35] reported that the flexure strength of hot pressed alumina changed from 350 MPa to more than 1 GPa when it was reinforced with only 5 vol% of SiC particles with an average size below $0.3 \,\mu\text{m}$. The fracture toughness also increased from 3.5 MPa m^{0.5} to 4.8 MPa m^{0.5}. In addition, these nanocomposites has excellent high-temperature properties. For instance, its creep rate at 1200°C is about three orders of magnitude lower than that of alumina. Chae et al. [36] produced by spark plasma sintering alumina reinforced with 20 vol% nano-SiC exhibiting flexural strength of 812 MPa and average fracture toughness of 3.6 MPa m^{0.5} compared with 663 MPa and 2.95 MPa m^{0.5} for the pure alumina compact, respectively. Flaw healing, machining induced surface compressive stresses, refinement of matrix grains because of the SiC nanoparticles and tightening of the grain boundaries by the compressive stress field created by the intragranular nanoparticles embedded in the alumina grains are believed to be the main strengthening mechanisms. The grain refinement in alumina has been attributed to a decreased grain boundary mobility and retarded grain growth of alumina caused by SiC particles. Indeed, the diffusion at the Al₂O₃/SiC interface is slow due to the strong directional bonding of both Al₂O₃ and SiC [42]. In addition, fracture mode changes from mixed inter/transgranular in pure alumina to pure transgranular within the nanocomposites, because of the dispersion of the nanoparticles within the matrix. This was explained by Levin et al. [38] as a consequence of the tensile residual stresses field which develops in the matrix

around intragranular particles because of the thermal expansion mismatch. In polycrystalline alumina, tensile residual microstresses are expected at some grain boundaries because of thermoelastic anisotropy. These tensile microstresses can promote intergranular fracture in monolithic alumina. SiC particles included in alumina matrix grains should create local compressive stresses on grain boundaries thus strengthening the boundaries. The formation of stress fields around the silicon carbide particles is based on the differences in thermal expansion of the materials, which causes radial compressive stresses around silicon carbide particles upon cooling. The stronger Al₂O₃/SiC interface bonding with respect to Al₂O₃/Al₂O₃ boundaries (the magnitude of interfacial fracture energy between SiC and Al₂O₃ is over twice the Al₂O₃/Al₂O₃ grain boundary fracture energy) can also be taken into account as inhibiting the crack to propagate along the interface. The residual stresses deflect the crack towards the intragranular particles, promoting transgranular fracture in the matrix. The change in fracture mode can also account adequately for the increase in fracture toughness in these nanocomposites. Only in the case of elongated and irregular alumina grain morphology, obtained by adjusting SiC content and presence of impurity, a T-curve behaviour could also be considered as toughening effect [37]. In fact the T-curve in nanocomposites is less apparent respect to alumina because of the matrix grain size decrease that impair grain bridging.

Strength and fracture toughness of alumina can be increased also by the inclusion of micrometric SiC particles. Zhang et al [42] observed that hot pressed alumina with 20 vol% SiC particles, with average size equal to 2.7 μ m, shows strength and toughness higher than that of monolithic alumina by about 20% at ambient temperature while at 1200°C the increase is of about of 30% and 70% respectively. The strengthening and toughening effect is higher for higher SiC contents. These particulate reinforced alumina matrix composites display improved fracture toughness due to crack tip shielding, crack branching and crack deflection. Micrometric SiC particles are usually allocated at the grain boundaries, which results strengthened by the strong SiC/Al₂O₃ interfaces, leading to a typical fine and equiaxed morphology of alumina grains and a transgranular fracture mode of the composite.

2.2.4 Alumina/silicon carbide hybrid composites

The addition of nanometre-size SiC particles within alumina matrix grains has been found to achieve a remarkable improvement in fracture strength, reliability and high temperature deformation resistance respect to pure alumina. However the significant increase in fracture toughness was difficult to achieve in Al₂O₃/SiC nanocomposites. One possible solution of overcoming this disadvantage is to add a third phase into nanocomposites, since the addition of reinforcement with high aspect ratio leads to a large increase in fracture toughness. According to this idea, fully dense SiC platelets reinforced Al₂O₃/SiC nanocomposites exhibiting improved strength, as high as 700 MPa, fracture toughness, with up to 8.5 MPa m^{0.5}, T-curve behaviour and creep resistance were fabricated by conventional powder mixing process and hot pressing [43].

2.2.5 Sintering of alumina/silicon carbide composites

Alumina produced by conventional powder routes can be completely densified in air at 1550°C while higher temperatures are necessary to sinter Al₂O₃/SiC composites. Indeed, diffusion at the Al₂O₃/SiC interface is slower than at the Al₂O₃/Al₂O₃ interface due to the strong directional bonding of both Al₂O₃ and SiC. Since densification in alumina is controlled by grain boundary diffusion the presence of intergranular SiC limits densification [42]. Consequently, work has been carried out into the use of sintering aids which lower the sintering temperatures, enhance diffusion rates or allow for faster sintering by creating a liquid phase [44-47]. Y_2O_3 and MgO have been investigated as sintering aids for Al₂O₃/SiC composites both individually and together. In alumina ceramics, it is well known that MgO is able to inhibit discontinuous grain growth and to promote sintering which leads to full density [48]. On the other hand, a small addition of Y_2O_3 can enhance the densification rate but accelerates the grain growth and is not so good for densification of alumina [46]. However, yttria enhanced the sinterability of the Al₂O₃/SiC composites without any substantial microstructural degradation. Pillai et al. [46] found the most dramatic effect was with 1 wt% Y2O3, with increasing density of a Al₂O₃/5 vol% SiC nanocomposite from 92% to 99% at only 1550°C.

Cock et al. [44] produced fully dense fine grained $Al_2O_3/5$ vol% SiC nanocomposite with an yttria content of 1.5 wt% and a sintering temperature of 1600°C. The enhancement of sintering by yttria in the Al_2O_3/SiC composites is because of the reaction of silica on the surface of the SiC particles (the surface of SiC particles is usually covered by a 0.3–0.7 nm coating of native amorphous silica [49]) with alumina and yttria and possibly other impurities to increase Si and Y concentrations in Al_2O_3/Al_2O_3 grain boundaries producing a grain boundary composition with relatively high diffusion rates at the used sintering temperatures. Discrete regions of $(3Y_2O_3:5Al_2O_3)$ yttrium aluminum garnet (YAG) could form within the alumina grains at the highest yttria content, probably precipitating upon cooling from a multicomponent eutectic liquid, with melting temperature below 1700°C. Unfortunately, the formation of low melting liquid phases due to sintering aids are detrimental to high temperature properties of these composites.

Therefore, high sintering temperatures above 1700°C, in Ar or N₂ as inert atmospheres used to avoid SiC oxidation, are usually required in fabricating Al₂O₃/SiC composites. On the other hand, it has been reported that in conditions of high temperature and low oxygen partial pressure, significant weight losses of the composite samples and several deleterious reactions like alumina decomposition, formation of carbides, oxycarbides, liquid phases and volatile species can occur [50– 56]. Barclay et al. [50] observed that, when sintering was conducted in a graphite resistance furnace with a flowing argon atmosphere, the problem of SiC oxidation was eliminated, however the compacts exhibited weight losses on the order of 1% and 10% at 1550°C and 1800°C respectively due to significant reduction of alumina. Assmann et al. [56] found weight losses above 30 wt% for the 25 vol% SiC content composite pressureless sintered at 1766°C under flowing Ar in a graphite furnace. Weight loss increases with sintering temperature and time, and SiC content. When sintering was conducted in N2, weight loss was reduced but phases as AlN, E-SiAl₇O₂N₇ and Al₁₁O₅N were formed. Moreover, a permanent melt with the composition of the eutectic in the Al_2O_3/Al_4C_3 system or a silicate glass due to the reaction between Al₂O₃, Al₄C₃ and SiC can be produced [55]. Misra [54] pointed out the effect of C and SiO₂ content in SiC liquid phase sintering and showed that the involved major gaseous species are CO, Al₂O, SiO and Al vapour. Jackson et al.

[53] reported that sintering SiC with mixtures of Al_2O_3/Al_4C_3 to form Al_2OC or a liquid phase is accompanied by a loss in weight which contributed to a reaction between Al_2O_3 and SiC to produce gaseous SiO, Al_2O and CO. Also Gadalla et al. [51] proved that alumina reacts with SiC to form, above 1700°C, Al_2OC and Al_4O_4C as condensed phases and SiO and CO as gaseous species. Baud et al. [57] made a complete thermodynamic analysis of the vaporization behaviour of SiC/Al_2O_3 and SiC/Al_2O_3 samples in a open system at 1200–2300K concluding that vaporization occurs following the fundamental following reactions:

$$Al_2O_3(s) + SiC(s) \leftrightarrow Al_2O(g) + SiO(g) + CO(g)$$
 React. (2.1)

$$Al_2O_3(s) + 2SiC(s) + Al_2O \leftrightarrow 2SiO(g) + 2CO(g) + 4 Al(g)$$
 React. (2.2)

Therefore, the main gas species are Al(g), Al₂O(g), SiO(g) and CO(g). The relative amount of the constituent solid compounds changes with time. For alumina rich samples the mixture tends toward pure alumina. When taking into account additional graphite, the CO(g) partial pressure increases and additional phases like Al₄O₄C, Al₂OC or Al₄SiC₄ can occur. These results leads to the affirmation that a control of the sintering conditions of the Al₂O₃/SiC system is essential.

In view of the difficulties encountered with pressureless sintering, hot pressing has been used to densify these composites [11,26]. Conventional powder processing, polymer precursor or sol-gel processing routes followed by hot pressing at 1550–1800°C and 20–40 MPa under Ar or N₂ atmospheres are used to obtain fully densified Al₂O₃/SiC composites. More innovative routes such as spark plasma sintering have also been investigated. Spark plasma sintering allows to reach theoretical densities at lower temperatures respect to hot pressing with higher rate of densification [36]. This enhancement was explained thanks to an acceleration of the diffusion process due to additional mass-transport mechanisms induced by the spark plasma. In addition, lowest temperatures as a function of SiC content have been observed and attributed to the difference of thermal conductivity between Al₂O₃ and SiC. Generally the thermal conductivity of SiC is higher than that of Al₂O₃ especially at elevated temperatures. Therefore, the addition of SiC might be expected to promote heat transfer from the graphite die to the compacts.

2.3 Ceramic laminates

2.3.1 Laminates with improved mechanical behaviour

Reinforced microstructures exhibiting toughening mechanisms have been presented in the previous paragraphs. Unfortunately, numerous restrictions which limit the use of ceramic composites for structural applications can be considered. The main problem regard the high costs of composite processing and starting materials, since a careful control of the microstructure and of its homogeneity is required. Degradation phenomena, involving the change of microstructure with time, can happen in service that decrease the toughening efficiency. A partial strength scatter, due to a residual dependence on starting crack size, still remains. For these reasons, today the arrangement of ceramic layers in laminated structures is the most promising route to improve the mechanical and tribological performances of ceramics.

Laminates are products that possess material composition, structure and microstructure which change with position in a regular manner. Typical applications of laminated ceramics include solid oxide fuel cells, electronic substrates, multilayered ceramic packages, gas sensor devices, filters, thermal barrier coatings and laminates with improved mechanical properties. The last item is the application of relevance in the present work. One of the main advantages of ceramic laminates with respect to traditional composites regards the reduced tendency to debonding and degradation phenomena occurring at the phase boundary since any residual stress is distributed within a larger volume. Interphase adhesion is higher when the structure changes in a gradual manner. In addition, the material can be improved by a second phase not in its whole volume but rather only where the tensile stresses are higher. In recent years, there has been considerable interest in the mechanical behaviour of a variety of multilayered ceramic composites. In the following paragraphs a brief summary of the state of the art of ceramic laminates with improved mechanical behaviour is presented, setting apart laminates with mechanical behaviour improved by toughening mechanisms, as crack bridging or crack deflection, and laminates characterized by the presence of residual stresses.

2.3.2 Laminates with mechanical behaviour improved by toughening mechanisms

2.3.2.1 Metal/ceramic laminates

Toughness enhancement could be obtained in metal/ceramic laminates where ceramic layers are alternated with metallic layers. As in the case of composites with ductile second phase crack tip shielding mechanisms are promoted. The toughness increase is controlled by the closure exerted by the metallic bridging layers astride the crack in the ceramic layers. Mekky et al. [13] produced a Ni/Al₂O₃ multilayer exhibiting a T-curve behaviour. In spite of the metallic nature of some layers the study of these laminates can be performed within the domain of Linear Elastic Fracture Mechanics if a well bonded interface exists.

2.3.2.2 Porous and weak interlayers

As discussed previously, the incorporation of fibrous reinforcements in a ceramic matrix is an easy way to create fiber/matrix interfaces with low fracture resistance that represent preferential paths for the propagating cracks. The presence of such weak interfaces increases the fracture resistance of the ceramic. Nevertheless, the fabrication of fiber reinforced ceramic is time consuming, complex and expensive. Increased toughness, T-curve behaviour as well as non catastrophic fracture behaviour have been also observed in laminates by introducing porous or weak interlayers to promote low-energy paths for growing cracks. Indeed, when weak interlayers are alternated with stronger ceramics layers the rupture occurs by crack propagation normally to the strong layer plane and then by crack deflection at an angle of 90° inside the weak interlayers (Figure 2.12 (a)). The typical loaddisplacement curve of these laminates (Figure 2.12 (b)) presents an initial linear trend, similar to the one observed for homogeneous ceramics, up to a peak load. The first load drop arises from a crack initiating from some surface defects and growing in the through thickness direction. Then the crack is arrested and deflected by the adjacent weak interlayer. Interfacial delamination and increasing of measured load until some new cracks form in the second strong layer are allowed. Such a sequence is repeated in the other strong and weak layers.



Figure 2.12: Al₂O₃-based multilayer with SiC weak interfaces. (a) propagation of a major crack with deflection along the weak interfaces. (b) measured and predicted load displacement curve of a specimen under flexure. (Adapted from [14,15]).



Figure 2.13: Al_2O_3 -based laminate with Al_2O_3 porous interlayers. The crack penetrating into porous interlayer undergoes deflection and branching. (Adapted from [16]).

She et al. [14,15] have fabricated multilayered Al_2O_3 ceramics with weak SiC interphases by extrusion molding and hot pressing. Due to the crack deflection mechanism the bending strength, toughness and fracture energy were respectively 563 MPa, 15.1 MPam^{0.5} and 3335 J/m². Finding a proper interface material for any given ceramic is the main shortcoming of these laminates with weak interfaces. A similar fracture behaviour could be obtain in a laminate where dense and porous layers are alternated, the latter playing the role as weak layers [16]. Controlled porosity is introduce in the weak layers by adding starch particles to slurry in slip based processes and consequent burn-out. This solution satisfy the requirements for chemical compatibility of interfacial materials and avoid the building up of internal stresses due to differences in thermal expansion coefficients which can be source of delamination during fabrication. Crack deflection, microcracking and branching, responsible of the toughening effect, have been observed within such systems (Figure 2.13).

2.3.2.3 Laminates with two strong outer layers and a tough inner layer

As described before, the development of reliable ceramics for structural applications has been approached from two different directions. The first approach is to develop ever stronger materials through processing and microstructural refinements. These techniques typically improve strength but still leave the material with a low toughness. The other approach is to activate the T-curve behaviour inducing toughening mechanisms as in composite materials. This will typically improve the toughness and the strength for large initial flaws. However these improvements are often achieved at the expense of strength for small flaws. This unfortunate trade-off between strength and toughness has lead to the development of a trilayer laminated composite which exhibit the high strength of the surface material for small flaws and the high strength of the tough body material for larger flaws [58]. According to this approach, Cho et al. [59] produced a laminate containing surface layers consisting of relatively fine, equiaxed a-SiC grains, designed for high strength, while the inner layer is made of elongated α -SiC grains, designed for high toughness. Chemical compatibility and strong bonding between layers has been also achieved. Improved strength, toughness and damage resistance

has been achieved with this three-layer ceramic laminate.

2.3.3 Laminates with mechanical behaviour improved by residual stresses

2.3.3.1 Residual stresses in laminates

Residual stresses can be defined as those stresses that remain in a body after manufacturing in the absence of any applied external load or thermal gradients. The main distinctive characteristic of residual stresses is that self-equilibrium must be maintained in any free standing body, which means that the presence of a tensile stress in the component is balanced by a compressive stress elsewhere in the same body. These stresses can generate in the body through (i) thermal expansion or sintering rate mismatch, (ii) local dilatations or deviatoric strains occurring during chemical reactions or phase transformations with molar volume changes, and (iii) differential plastic deformation like that occurring during grinding operations [60]. The introduction of stresses within the material is an alternative procedure to improve mechanical performances in ceramics. For example, surface compression is usually induced in tempered glass, used for glass windows, lateral or rear car windows, ophthalmological lenses and other high strength applications. To produce tempered glass, the glass plate is heated to a temperature high enough to allow adjustments to stresses among the atoms, then is quickly cooled down. The surface contracts because of the drop in temperature and becomes rigid, while the center is still hot and can adjust its dimensions to the surface contractions. When the center cools and contracts slightly later compressive stresses are produced at the surface and tensile stresses are produced in the center. A considerable deflection must be applied to the glass before tensile stresses can be developed in the surface of the glass where cracks start. In effect, since the compressive stresses must be overcome first, the overall strength of the glass is enhanced as much as 300% [1].

The impediment to free deformation at the base of residual stresses creation is known as constrain effect. The same effect is present in an orthotropic laminate made of cosintered layers of different composition and perfectly adherent one to each other. Orthotropy happens when each layer in the laminate is homogeneous, isotropic, linear elastic and the stacking order of the laminae satisfy the symmetry conditions. Orthotropic laminates exhibit response to loading similar to that of homogeneous plate and no warping during in-plane loading is produced [61]. If perfect adhesion between laminae is assumed, each lamina must deform similarly and at the same rate of the others. The mismatch between the free deformations or deformation rates of the single lamina with respect to the average value of the whole laminate gives origin to residual stresses. More precisely, during cooling, the difference in deformation due to the different thermal expansion coefficient of the components, is accommodated by creep as long as the temperature is high enough. Below a certain temperature, which is called the "stress free" or "joining" temperature, the different components become bonded together and internal stresses appear. Indeed, the stress free temperature represents the temperature below which the material can be considered to behave as a perfectly elastic body and visco-elastic relaxation phenomena do not occur [62]. In each layer, the total strain after sintering is the sum of an elastic component and of a thermal component [63]. In addition, if the laminate thickness is smaller respect to the other dimensions, each lamina can be considered, far away from the edges, in a biaxial stress state with no stress acting perpendicular to the lamina plane.



Figure 2.14: Edge crack of length c in a semi-infinite body in presence of a generic residual stress distribution $\sigma_{res}(x)$.

The magnitude of these residual stresses can be tailored through an accurate choice of system geometry and layers composition.

We consider here an infinite plate with a generic non uniform stress distribution $\sigma_{res}(x)$ acting along the direction x perpendicular to the plate surface on a through-thickness sharp crack of length c (Figure 2.14). The stress intensity factor $K_{I,res}$ related to the stress distribution can be estimated by using the weight function approach:

$$K_{I,res} = \int_{0}^{c} \sigma_{res}(x) h\left(\frac{c}{w}, \frac{x}{c}\right) dx \qquad Eq. (2.8)$$

where h is a weight function, w is the plate width and the other symbols have the standard meaning [6]. The weight function is a geometric function that satisfy the singularity conditions at the crack tip. It is tabulated in literature for many geometries and loading conditions. If the residual stresses are separated from external loading, the term due to their presence can be included in the material fracture resistance to obtain the so called apparent fracture toughness K_{Lapp} or T:

$$K_{I,app} = K_{IC} - K_{I,res} \qquad Eq. (2.9)$$

The crack propagates under the external load when the value of such characteristic is reached. In the case of negative compressive residual stresses the second term in Eq. (2.9) is positive and the apparent fracture toughness increases with respect to K_{IC}. This beneficial effect can lead to a T-curve behaviour [23,64]. As described in the following paragraphs, several laminated ceramic structures with improved mechanical behaviour, due to the introduction of residual stresses, have been developed.

2.3.3.2 Laminates with two compressive outer layers and a tensile inner layer

Surface macroscopic compressive stresses can be introduced in a laminate to reduce the intense tensile stresses acting on the crack tip and to hinder the surface cracks propagation with an effect similar to what discussed in tempered glasses [65,66]. Therefore, increased strength, hardness and flaw tolerance can be achieved. For this three-layer design there is only one compressive layer to act as barrier and to arrest cracks. However, multilayered structure is of further importance to stop cracks more effectively.

2.3.3.3 Threshold strength laminates

Laminates presenting threshold strength, namely a stress below which the probability of failure is zero for any starting defect dimension, have been successfully produced by alternating thin compressive layers and thicker tensile layers. Indeed, Rao et al. [18] showed that alternating thin compressive layers between tensile layers can truncate the statistical strength distribution of brittle materials. Indeed, the crack starting in one of the tensile layer and propagating normally to the layer plane increases its length up to equate the thickness of the tensile layer itself and then slow down since the compressive stresses hinder the further propagation. Within the compressive layer the crack propagation becomes stable and all defects reach the same final length before failure. Hence, the strength shows threshold value. Other research groups have demonstrated that this kind of laminates [19,66,67] presents a T-curve behaviour, damage tolerance and reduce strength scatter. Notwithstanding the high scientific interest in such laminates, they have strong limitations: fundamentally, the threshold strength only occurs when cracks extend perpendicular to the compressive layers, so they can be used only with specific orientations to the applied load. In addition, if a pre-existent defect larger than the unit cell exists, the actual strength is lower then the threshold value. Finally, a limit to the maximum strength, which can be designed does exist, since an increase of its value involves an increase of the amplitude of compressive stresses. As a consequence, cracks can spontaneously develop in the tensile layers.

2.3.3.4 High reliability ceramic laminates by design

To obtain a T-curve behaviour able to enhance mechanical reliability it is not sufficient to introduce residual stresses in the material. Sign and intensity of the residual stresses have to vary in a controlled and designed way as a function of the position. Sglavo and Green [64] have demonstrated that the creation of a residual stress profile with the maximum compression at a certain depth from the surface of a material can allow the stable growth of surface flaw and their arrest, up to this specific depth, before the final fracture. The strength scatter is reduced as the strength turn out to be independent on the initial cracks length and higher. The underlying idea can be traced back to the observation of biological structures in which the most performing parts of the material are located in regions that experience the highest stresses. Surface flaws, usually generated both in fabrication and in service, are the typical critical defects in ceramic materials subjected to bending conditions. Therefore, precisely the ceramic surface has to be engineered to tolerate at the same time external loads and the flaw population. These concepts have found practical applications in Engineered Stress Profile (ESP) glasses [6,20,25], and in oxides based ceramic laminates [22-24]. The production of these innovative ceramic laminates is economic because based on common ceramic materials (alumina, mullite, zirconia) and inexpensive conventional fabrication methods as tape casting, lamination and cosintering. As an example, the architecture of one alumina (A)/mullite (M) engineered laminate with increased reliability respect to monolithic alumina is shown in Figure 2.15. For this AM engineered laminate, a Weibull modulus equal to 17 was obtained, higher than the value equal to 12.1 calculated for alumina monolithic laminate [22]. A residual stress variation is introduced into the engineered laminate during cooling after cosinterng of the constituent layers characterized by different thermal expansion coefficient. This multi-step residual stress profile is composed of a tensile layer on the outside, that permits to extend toward the surface the stable crack growth interval, and a number of compressive laminae in the inner zone with the maximum compression layer at a specific depth from the laminate surface (Figure 2.16). The laminate architecture could be built, varying the nature and the thickness of the single lamina and the stacking order in the multilayer, to exhibit a determined residual stress profile and, therefore, a T-curve behaviour (Figure 2.17). A stable crack growth interval, the presence of a threshold stress and an improved strength are the effects of the introduction of this toughness variation inside the material.



Figure 2.15: Architecture of an alumina (A)/mullite (M) engineered laminate. Layers composition (mullite content as vol%) and thickness are reported. Dimensions are not in scale. (Adapted from [24]).



Figure 2.16: Residual stress profile of the engineered laminate represented in Figure 2.15 [24].



Figure 2.17: Apparent fracture toughness for the engineered laminate represented in Figure 2.15 [24].

The approach used for the laminate design is summarized in the following mathematical analysis. Considering a thin orthotropic multilayer with strong interfaces between the n layers, the biaxial stress state in each layer, generated by thermal contraction during cooling, can be calculated on the basis of equilibrium of forces, compatibility of the deformations related to constrain and the constitutive model:

Self-equilibrium
$$\sum_{i=1}^{n} \sigma_i t_i = 0$$
 Eq. (2.10)

Compatibility
$$\varepsilon_i = e_i + \alpha_i \Delta T = \varepsilon$$
 Eq. (2.11)

Costitutive model
$$\sigma_i = E_i^* e_i$$
 Eq. (2.12)

where the subscript i represents the rank of the generic layer and σ is the acting stress, t is the thickness, ε is the deformation, e is the elastic strain, α is the thermal expansion coefficient, E* is the Young modulus in the case of biaxial stress state, expressed by Eq. (2.13), and ΔT is the temperature difference, expressed by Eq.

(2.14):

$$E_{i}^{*} = \frac{E_{i}}{1 - v_{i}}$$
 Eq. (2.13)

$$\Delta T = T_{SF} - T_{RT} \qquad \qquad Eq. (2.14)$$

E is the Young modulus in uniaxial stress state, v is the Poisson's modulus, T_{SF} is the stress free temperature and T_{RT} is room temperature. The linear system of Eq. (2.10), Eq. (2.11) and Eq. (2.12) represent a set of 3n+1 equations and 3n+1 unknowns that can be easily solved. The resulting residual stress in the generic layer i is equal to:

$$\sigma_{\text{res},i} = E_i^* (\overline{\alpha} - \alpha_i) \Delta T \qquad \qquad Eq. (2.15)$$

where $\overline{\alpha}$ represents the average coefficient of thermal expansion of the whole laminate expressed as:

Since the stress level in Eq. (2.15) does not depend on stacking order, the calculation is valid for each sequence of laminae, providing the symmetry condition is maintained. In order to understand the effect of residual stress intensity and location on the apparent fracture toughness of an edge crack in a semi-infinite body, Sglavo et al. [22,23] have analyzed some special cases of profile: step profile, square wave profile and two square waves based profile. An inductive approach and the superposition principle have been used to calculate the T-curve for a general multistep profile. In the case of a laminate composed of n layers with constant residual stresses $\sigma_{res,i}$ (Figure 2.18), the apparent fracture toughness $K_{Lapp,i}$ within layer i in the interval $[x_{i-1}, x_i]$ has been calculated as equal to:

$$K_{I,app,i} = K_{IC,i} - \sum_{j=1}^{i} 2Y \left(\frac{c}{\pi}\right)^{0.5} \Delta \sigma_{res,j} \left[\frac{\pi}{2} - \arcsin\left(\frac{x_{j-1}}{c}\right)\right]$$
$$(x_{i-1} < x < x_i)$$
$$Eq. (2.17)$$

$$\Delta \sigma_{\text{res},i} = \sigma_{\text{res},i} - \sigma_{\text{res},i-1} \qquad \qquad Eq. \ (2.18)$$

where i indicates the layer rank and x_j is the starting depth of layer j, being Y =1.12147.



Figure 2.18: Crack model considered by Sglavo and co-workers [23]

The latter assumption is not rigorously true for non-uniform loading since Y maintains a slight dependence on x/c but such approximation allows to simplify the calculations without lose of generality. Eq. (2.17) represents a short notation of n different equations since the sum is calculated for a different number of terms for each i. The sequence of the apparent fracture toughness of the layers with the specified residual stress profile lead to a T-curve behaviour. The degrees of freedom

to produce the desired T-curve are 2n-2 since n equation with 2n parameters $(x_i, \Delta \sigma_i)$ are now available and two conditions have to be satisfied (force equilibrium and equivalence between the sum of single layer thickness and the total laminate thickness). In addition, the calculations can be referred to the semi-thickness as the laminate is symmetric. Referring to the most internal between the tensile layers placed at the surface as k and to the most compressed layer as 1 it is possible to determine the stable crack growth interval $[x_k, x_l]$, the threshold stress σ_{th} and the strength σ_b of the laminate:

$$\sigma_{\rm th} = \frac{\min(K_{\rm I,app,k}, K_{\rm I,app,k+1})}{Y(\pi x_k)^{0.5}} \qquad Eq. (2.19)$$

$$\sigma_{\rm b} = \frac{\max(K_{\rm I,app,1}, K_{\rm I,app,1+1})}{Y(\pi x_1)^{0.5}} \qquad Eq. (2.20)$$

Therefore the input parameters of laminate design are the coefficients of thermal expansion, Young's moduli, Poisson's ratios, fracture toughness and the layers thickness. Another important but experimentally unknown input parameter is the stress free temperature T_{SF} assumed as equal as 1200°C, while room temperature is 25°C [62]. The presented model is very simple and approximated but the error in the calculation of the apparent fracture toughness in each layer has been estimated as being as less than 10% [22]. These innovative laminates possess high mechanical reliability and equivalent mechanical characteristics along any loading orientation. These properties make these laminated bodies as natural candidates for structural applications as in the case of load bearing components in automotive and aircraft industry, biomedical prosthesis, chemical plant linings and safety systems.

2.3.4 Defects in laminates

The constrain effect developed in cosintering layers within a laminate with strong interfaces is responsible of the arising of residual stresses within the multilayer. If this effect is sufficiently higher, porosity and deleterious defects can also outcome. Some specific defects with scale comparable with the layer thickness are delamination or debonding, channel cracking or tunnelling, edge cracking and warping [68].



Figure 2.19: Typical defects observed in laminates: (a) delamination; (b) channel cracking; (c) edge cracking. (Adapted from [68,69]).

Delamination (Figure 2.19(a)) involves an evident separation between adjacent layers and occurs when the adhesion forces between the layers in the laminate are low. This problem can be solved by reducing the thermal/sintering mismatch or by improving the interlayer adhesion.

Channel cracking (Figure 2.19(b)) is a typical defect associated to the presence of tensile stresses in a layer. The cracks propagate normally to the layer plane with a quasi random orientation in the plane itself. Similar consideration as for delamination can be advanced to avoid such defect.

Another well-known phenomenon observed in high compressed layers is edge cracking (Figure 2.19(c)). Although these layers contain biaxial compressive stresses deep within the thin layers, tensile stresses arise wherever the compressive layer is truncated by a free surface. These tensile stresses are perpendicular to the compressive layer and have an absolute magnitude equal to that of the compressive stress at the centre-line. The tensile stresses decrease to zero at a distance from the surface equal to the thickness of the layer, namely the tensile stresses are highly localized near the surface of the compressive layer. When the thickness of the compressive layer is greater than a critical value, the tensile stress gives rise to a crack that extends along, or near, the centre-line to a depth corresponding to approximately the thickness of the compressive layer. Consistent with the theory developed by Ho et al. [69], the centre-line crack, called an edge crack, is only observed when either the compressive stress or the thickness of the compressive layer exceeds a critical value. For the fixed value of compressive stress, the critical compressive layer thickness (t_c) required for edge cracking is given by:

$$t_{c} = \frac{K_{IC}^{2}}{0.34(1+\nu)\sigma^{2}} \qquad Eq. (2.21)$$

where K_{IC} , v, and σ are the fracture toughness, Poisson's ratio and the stress of the thin compressive layer material respectively.

Distortions, curvature and uneven modifications of the planar geometry of symmetric laminates are also possible upon cooling. These warping effects are usually related to local differences in the layer thickness occurring somewhere in the laminate. The resulting lack of moment balance produce a curvature in the material to satisfy equilibrium.

2.3.5 Processes suitable to produce ceramic laminates

Melting is not a suitable fabrication technology for ceramics since, generally, their melting temperature is too high and degradation phenomena occur earlier. Sintering after powder forming of green products is the most common technique involved in the production of ceramics. The typical classification for ceramics processing regards the physical state of the forming material: dry powder or fluid suspension, or slip, in which the powders are dispersed. Some organic or inorganic additives can be present in both cases, the distinction remaining the actual presence of a fluid solvent. The forming process is usually chosen according to economic factors and shape, dimensions and final characteristics that the product has to satisfy. Ceramic sheets are used in many widely different end products such as substrates for electronic circuits, discrete electrical devices, multilayered cofired packages for integrated circuits, multilayered assemblies such as fuel cells and plate electrodes. Green tapes are also used as intermediate steps in the production of more intricate shapes. Several processes are used to form large area and thin, flat ceramic

sheets and then laminates; pressing, electrophoretic deposition, tape casting, slip casting, rolling and other, followed by sintering or hot pressing. Simply adaptations of the methods used to produce traditional ceramics and also new solutions proposed and developed rightly for the purpose are employed. All these processes have in common the capability to originate a predetermined gradient in the green structure of the laminate, which give rise to a spatial variation in the structure of fired ceramic. In the following paragraphs, a brief overview about the most techniques involved in the production of multilayers is presented. Competing processes to make similar flat ceramic parts include extrusion, vibrational induced particle segregation, multiphase jet solidification, reactive hot pressing, infiltration, interdiffusion of cosintering materials will not be explored here since they are not widely used for this purpose and they have many serious limitations [70-72]. A separate subject regards the techniques used to produce thin coatings, like CVD (Chemical Vapour Deposition), PVD (Phase Vapour Deposition) and sputtering. All the deposition methods can be also considered for laminates fabrication, the main restrictions remaining the maximum thickness, which can be obtained in a single step, the deposition rate and the costs.

2.3.5.1 Dry powder-based processes

Cold pressing of ceramic powders followed by sintering [73] can be used to produce laminates. Powder feed is composed of granules of different size and deformability mixed together to obtain the maximum compact density and the minimum porosity volume. Little amount of water or binder and other organic additives are generally added to promote the relative motion between the powders, arising during pressing. Cold pressing could be uniaxial, when the pressure is applied in only one direction, or isostatic, when pressure is applied in each direction with equal intensity. The desired structure gradation in the space, useful to obtain laminated structures, is actually obtained by stacking batches of different compositions. However, layers thickness and dimensional tolerances are much more difficult to control when thin layers have to be produced. As for the homogeneous ceramics, the compressed green material has then to be sintered to obtain a fired and dense material showing the same graded structure present in the pre-form. Pressing 58 is today the most widely practiced forming process for reasons of productivity and the ability to produce parts ranging widely in size and shape.

Roll compactions [74] is another dry pressing process in which a prepared powder is continuously pressed between two rollers to form flexible green tapes. The tape made with this process is then immediately available for cutting or handling. Sintering process is needed to obtain the final product. The advantage of rolling, as a method of green layers production, are that it allows easy thickness control, achieves high green density of the tapes, and requires a rather low amount of solvent and organic additives as compared to other methods. Rolling lends to higher volumes of materials but require more rigid powder preparation. Therefore it is not often used for new material development or small quantity production.

Hot Pressing (HP) and Hot Isostatic Pressing (HIP) [73] can be used to densify ceramics in a more effective way respect to simple cold pressing followed by sintering. A sintered product is directly obtained by performing uniaxial powder pressing (HP) in a refractory die and sintering at the same time. Conversely, with hot isostatic pressing (HIP) a product previously sintered to the final stage of sintering is subjected to a hot pressurized gas. These techniques are pressure assisted sintering processes generally used to produce high temperature melting materials, when a sintering aid or grain growth inhibitor is unacceptable. The mechanical pressure used in this techniques, usually in the range of 10–200 MPa, can increase the driving pressure for densification by acting against the internal pore pressure without increasing the driving force for grain growth. Indeed, the main effects for the enhancement of sintering in these processes are thermal diffusion and plastic flow due to the high pressure. Therefore, respect to conventional sintering technology, they allow to obtain high density products with fine microstructure at lower temperatures. The industrial use of hot pressing is limited because the productivity is relatively low, restricted in size and geometry of the samples, and the die maintenance is expensive. However, today, hot pressing is the main sintering technique to produce alumina/silicon carbide composites.

Recently, the Spark Plasma Sintering (SPS) process [36,75,76], also known as Pulsed Electric Current Sintering (PECS) has attracted a great deal of interest as a new cost-effective processing method for sintering and sinter-bonding, at considerably rapid heating rates, various kind of powder materials and laminated structures as, for example, TiN/Al₂O₃, SiC/TiC, Si₂N₄-SiC/BN-Al₂O₃ and HA/Y-TZP [77-79]. SPS is an innovative technology similar to the conventional HP process because mechanical pressure is applied during the heating stage. Nevertheless, in contrast to the conventional HP, in which the heat is provided by external heating elements, in SPS the heat is generated internally. In fact, a pulsed direct electric current passes through the graphite die and, depending on the electrical conductivity of the material to be sintered, also through the powder compact within the die itself. Such electrical current propagation significantly improves heat transfer by different mechanisms involving Joule heating, diffuse electrical field, spark plasma, and spark impact pressure, resulting in a currentactivated sintering. Spark plasma has a surface activating and cleaning effect on the particles being sintered and allows a rapid heating of the compact particles. The occurrence of a plasma discharge is still debated but it seems to be widely accepted that an electric discharge process takes place on a microscopic level. Therefore, SPS has several advantages over conventional sintering methods including high heating rates, lower processing temperatures, and short holding times, thus allowing the production of highly dense materials with improved quality and good control of grain coarsening.

Plasma-spray [70] is a well-known process used to produce thick coatings, like the thermal barriers on the blades in gas turbines. High tension is applied between two electrodes placed in a torch in such a way that the resulting electric arc promotes the transformation of the flowing gas in the plasma state. In front of the nozzle temperature can locally reach values as high as 30000 K. The ceramic powder is fed near the torch tip, where is heated, dragged by the gas flame and sprayed onto the substrate. The torch, moved by a robotic system, is used to focus the flame onto the substrate and to change the target position on the surface. Many parameters can be varied in order to modify the thickness, the structure and the microstructure of the sprayed material, including gas flow, powder feeding position and rates, distance between torch and substrate, substrate pre-heating and powder morphology. Plasma spray can work either in vacuum or in air, depending on the nature of the powders to be sprayed. Typically a porous structure and a rough

surface finishing is obtained by plasma spray, the coating thickness typically ranging from a few tens to several hundred of microns. Compared to other coating processes, plasma spray allows a high mass transport and thus a high speed deposition. Furthermore, layer thickness can be varied easily by adjusting experimental parameters and, contrary to pressing-based processes, no thermal treatment is required after spraying. Unfortunately, some restrictions are also present since a substrate to be coated is always required and no self-supported body can be produced. In addition, a residual porosity and a rough surface finishing of the sprayed layer can not be avoided.

2.3.5.2 Slip-based processes

Colloidal processing offers the possibility to produce strong and reliable ceramics of good quality through careful control of the initial suspension and its evolution during fabrication. This can be accomplished by reducing the size of the strength degrading heterogeneities, as inorganic and organic inclusions or agglomerates.

Among colloidal processing, tape casting [80,81] and lamination of different thin and flat ceramic layers to form thick specimens is a relatively simple and inexpensive process considered a valid route to produce green ceramic laminates. Tape casting has been widely used to develop ceramic substrate, multilayer structure capacitor, solid electrolytes, solid oxide fuel cell, and has been performed on several materials including alumina, zirconia, barium titanate, nickel, nickel oxide and piezoelectric materials. It is a wet forming method which consists in layering a slip containing the ceramic powders, onto a temporary rigid plane support by gravity flow occurring while the reservoir carrying the slip, called doctor blade, is moved with respect to the substrate. The relative motion between the reservoir and the substrate can be obtained either by moving the carrier film (stationary blade) or the reservoir itself (moving blade), while the slip flows through a controlled slit present in the bottom rear part of the doctor blade (Figure 2.20). The casted green tape is a single continuous sheet presenting a thickness much smaller than the other two dimensions.



Figure 2.20: Outline illustrating the tape casting process in the stationary blade configuration.

The slip, or slurry, is a complex fluid system formed by dispersing the inorganic materials with dissolvent organic binders, dispersants, plasticizers and surfactant in a solvent system. Each of the organic materials is added to the formulation to contribute certain properties to the slip and the dried tape. The production of a slurry for tape casting is a complex task involving the definition of a number of experimental parameters strictly correlated. This includes the choice of the nature and amount of all the ingredients in the slip recipe, the preparation method to obtain a well dispersed suspension and then a homogeneous slip to be cast, together with all the parameters associated to casting itself. The objective is to achieve the maximum solids loading in the slip in order to produce dense and good quality green tapes with good reproducibility. Ceramic powders used for tape casting commonly have an average particle size in the range of $0.3-3.3 \mu m$ and a specific surface area of about 2–11 m²/g [81]. The size distribution is dictated by the opportunity to improve the green homogeneity and density. The solvent or solvent blend has the function to originate a fluid system and to homogenise all the ingredients in the slip. Non-aqueous suspensions avoid hydratation of the ceramic powder and are faster drying thanks to high vapour pressure and low boiling point and heat of vaporization of the organic solvents. However, they require special precautions concerning toxicity and inflammability. Typically, organic solvent recovery systems are needed to control emissions of compounds into the atmosphere. On the other hand, water based solvent systems are attractive since they have advantages of incombustibility, non-toxicity and low cost, associated with the large amount of experience with the use of water in similar ceramic powder process. Unfortunately, thicker tapes are more difficult to make by using aqueous suspensions mostly due to problems in the drying process. In effect, water has the disadvantage of high evaporation latent heat and longer drying time, thus higher drying temperature are required when using aqueous systems. Also wettability can be a problem due to the high surface energy of water. Another difficulty is related to the production of good dispersion for slips which include two or more kinds of powders, especially when the particle size and density are quite different. A good powder dispersion is essential to obtain tape homogeneity and uniform shrinkage without grain coarsening during sintering. In the case of water based systems, an important role is played by the powder isoelectric point (IEP), also known as Point of Zero Charge (PZC), since pH intervals of mutual attraction between powders with different IEP can promote strong flocculation phenomena. When dispersed in water, particles exhibit proton exchange reactions and a non-zero surface electric charge is typically achieved at equilibrium, assuring an electrostatic repulsion between the particles. IEP represents the pH value corresponding to an average zero charge on the particle surface. This is the worst condition for dispersion, since no repulsion force exists to face the attractive Van der Waals interactions. When pH is higher than IEP, the charge on the surface is negative, while it is positive when pH is lower (Figure 2.21). In the case of powders with different IEP, it easy to see that in some pH range opposite charges can occur and promote a strong inter-particle attraction. Two general methods are used to produce the short-range, interparticle repulsive potential useful to obtain well dispersed slip. For each, a chemical route is used to shroud the particles with a barrier layer. In the first method, the barrier layer is produced with a cloud of ions: the density and thickness of the cloud is controlled by adjusting the pH and salt concentration. In the second method, the barrier layer is produced by attaching polyelectrolyte molecules to the surface. In this case, the thickness of the barrier layer is governed by the size of the chem-adsorbed molecule. The adsorption of such polyelectrolyte on the particle surface can shift the IEP

position (Figure 2.21) and favour the inter-particle repulsion.



Figure 2.21: Relative Acoustophoretic Mobility (RAM) for 16.7 wt% dispersion of A-16SG alumina in pure water with and without the polyelectrolyte Darvan C. (Adapted from [82])

Therefore, a dispersant is needed to promote and maintain stable the powder dispersion in the solvent. This effect is achieved by electrostatic repulsion, steric hindrance of adsorbed dispersant molecules or a combination of the two mechanisms. The optimum amount of dispersant is thus proportional to the powder surface area. The binder is a long-chain polymer or a colloid that provides strength and flexibility to green tapes after evaporation of the solvent through organic bridges between the ceramic particles. Binder selection depends on its viscosity, strength, glass temperature and burn-out atmosphere. A high molecular weight is desired in the binder for high toughness and strength and a low glass transition temperature. If present in sufficient amount, the binder represents a continuous polymeric matrix entrapping the ceramic powder thus allowing handling, storage and green machining 64

as cutting and punching. The binder should be compatible with the dispersant. should provide lubrication between particles and should not interact during solvent evaporation. In most cases, low molecular weight polymers are also added as plasticizers to increase the green deformability at room temperature. The combination of binder and plasticizer must be balanced to provide the required mechanical properties and to permit a high concentration of inorganic particles in the slurry. Two groups of substances mainly have been used as binders for aqueous tape casting of ceramics: cellulose ethers and vinyl or acrylic-type polymers [80]. The colloidal properties of acrylic polymer emulsions lead to slip formulations containing high solid contents in well-dispersed systems. Moreover, these emulsions have useful and unique characteristics such as low viscosity, internal plasticization and controllable crosslinking, which provide a good cohesion to the green sheet but with a low strain to failure. On the other hand, they include some surfactants in order to stabilize the emulsion which can promote foam formation. Other additives, including wetting agents to promote spreading of the slurry on the carrier substrate, homogenizers which contribute to a better surface quality and antifoaming agent to prevent foaming during mixing, can be used.

Milling, in particular wet ball milling or vibratory milling, is used to break aggregates and to disperse powder agglomerates as well as to mix and homogenize the organic additives. It is well known that mixing of the organic ingredients, in aqueous tape casting, is commonly accomplished by using a two-stage milling process [80,81]. The liquid, the powders and other additives of low molecular weight are mixed by using ball milling procedure for 12–24 h at a relatively higher viscosity at which shear forces are able to disperse agglomerates. Then, dissolved gas in the slurry is commonly removed in a close container under vacuum. Next, the binder and plasticizer are added and milling process is used to reduce the scale of inhomogeneity in the slurry without foaming or degrading the high molecular weight binder molecules. Before casting the slip is filtered to remove any residual coarse agglomerate or polymer cluster. Indeed, agglomerates and undissolved organic material must be finer than the thickness of the tape for proper forming and for ultimate thermal and mechanical properties. Due to the high solid content and to

the presence of organic polymers, the slip to cast presents usually a high viscosity and a pseudoplastic rheological behaviour (its viscosity decreases when shear rate increases). In some cases, time dependent phenomena as thixotropy can also be observed. The slurry is usually cast on a smooth polymeric tape carrier, as Mylar®, Teflon® or silicone, by the relative movement between the doctor blade and the carrier. The cast tape thickness can be easily controlled by adjusting the blade gap, the casting speed and the slip viscosity. Casting is followed by drying which has the main function to remove the solvent. Drving is usually performed in closed system or at open air, from room temperature to 85°C, with relative humidity from 50% to 70%. During this stage, the solvent escapes by diffusion and evaporation, while the solid phases (powders, binder and plasticizers) settle at the bottom. Flexible and deformable dried green sheets, with a typical thickness in the range of 25-1250 µm, are generally produced. To obtain a multilayered structure, the tape casting is followed by a lamination process where the layers stack is thermo-compressed to give the green laminate. The obtained bond strength between layers is important for maintaining product integrity during the sintering process. Lamination is usually performed at a temperature range of 50-150°C and pressures of 3-30 MPa. Then, the organic matter present in the green laminates is generally removed by a slow heating burn-out treatment before sintering. One of the main advantages of tape casting regards the good density and homogeneity of the green, which allows the production of a dense fired ceramic with a uniform microstructure. Some problems do exist associated to the anisotropy of the shrinkage during drying: solvent removal occurs in fact only from the top surface. The residual stresses due to substrate constrain can not be sustained when the thickness increases over some critical extent or when the binder is not properly plasticized, the main outcomes being cracks and defects produced in the green.

Sequential slip casting [83] is a simple modification of the slip casting method, which is performed in this case by batch. Gravity is always the force controlling the particle settling and the deposition rate can be adjusted by means of several parameters, the most important being particle size and slip viscosity. As for traditional slip casting, organic suspending agent can be used to the purpose. A tailored profile in the structure is constructed by a proper change of the batch

composition with time, by emptying and filling the mould with a new slip every time a new layer is desired. Also in this case layer thickness can be controlled easily by adjusting the settling time.

Conversely, in the case of sedimentation slip casting the graded structure is obtained by means of different settling rates of the slip components [84] and there is no need to a continuous change of the slip. A further evolution of the process is called graded casting: an automated procedure for mould feeding permits the formation of a continuous gradient in the composite [84]. With respect to tape casting, the binder content is limited and this is a substantial advantage since costs are reduced accordingly and the controlled burn-out phase is less critical. A drying phase follows to complete the solvent removal, which partially diffuses across the porous mould during casting. Large and complex shapes can be obtained quite easily, the main limitation regarding the overall duration required by the process.

Centrifugal consolidation is quite similar to the previous one. The main difference regards the driving force for the material deposition, which is here supplied by the centrifugal acceleration in place of gravity. In addition, a simultaneous move of the suspension medium also occurs in the opposite direction and no flow through the sedimented body is required for the solvent removal during drying. The deposition rate can be controlled by adjusting the rotational speed, while a limitation exists regarding the orientation and the shapes which can be processed. The technique seems very promising and is particularly suitable for bodies presenting an axial symmetry, like discs, tubes and shells. Small flat multilayered laminates have been also produced by placing the container in a radial direction, though a slight curvature in the green sample can not be avoided [72]. Selfsupported bodies can be also produced.

Electrophoresis [72] works by applying an external dc electric field to a slurry promoting the migration of charged particles to the opposite charged electrode. The particles must be well dispersed within the medium to show high electrophoretic mobility. Water is also used as solvent because it is polar, economic, ecological and safe. The electric field generated by the applied potential difference is the force controlling the deposition rate of material. At the electrode, the double layer which guarantees the repulsion of moving particles is distorted and short range attractive forces are developed. Then, particle transfers its charge to the electrode and remain attached to the growing layer, usually with a high packing density. A drying step is then required to remove solvent. The layer thickness vary typically from a few to a few hundred microns. A graded structure can be obtained by changing the slip or by using particles with different mobility, while the single layer thickness can be easily controlled by voltage application time.

Chapter III

Experimental Procedure

3.1 Material and process selection

3.1.1 Material selection

The aim of this work was to produce alumina/silicon carbide multilayered laminates presenting a T-curve behaviour arising from properly designed residual stress profile. According to the practical rules presented before, in order to generate residual stresses in the multilayer, it is necessary to use materials with different thermal expansion coefficients and sintering shrinkage. Since the sole thermal expansion mismatch between the materials is considered as the driving force for the production of residual stresses, the production of a multi step residual stress profile in a cofired laminate requires a range of different laminae, each one presenting a different thermal expansion coefficient. This can be easily achieved by producing several composites and by tailoring the thermal behaviour through the composite composition control.

Among laminated composites, one of the most studied system is the alumina/zirconia one [19]; alumina, zirconia and mullite have been already used as starting materials in the production of laminates exhibiting residual stress profiles and T-curve behaviour [22–24]. The material systems selected for the proposed study are alumina and silicon carbide because, in the range of temperature $25-1500^{\circ}$ C, alumina has a coefficient of thermal expansion of ~8·10⁻⁶°C⁻¹, while silicon carbide has ~5·10⁻⁶°C⁻¹ (Table 3.1). The reason for choosing alumina and silicon carbide as the constituent materials of ceramic laminates can be traced back to the fact that both materials are mutually insoluble, there are no intermediate phases, no solid state or eutectic reactions that could lead to material changes during the high temperature cofiring treatment, in inert and proper conditions; in addition, it is possible to obtain excellent bonding between the layers in the absence of

excessive diffusion between components. In addition, they present good refractoriness, high stiffness and good thermo-mechanical properties. These characteristics make the two materials interesting candidates for the composites production. Also the challenge in sintering these materials up to full densities with conventional or innovative technologies has been taken into account. According to previous works, previously presented, yttria has been selected as additive powder to enhance sinterability of the alumina/silicon carbide composites.

Table 3.1: Ceramic materials considered in this work. Density (ρ), Young's modulus (E), bulk modulus (B), shear modulus (μ) and thermal expansion coefficient (α) are reported.

Material	ho	Ε	В	μ	α
	[g/cm ³]	[GPa]	[GPa]	[GPa]	$[10^{-6} \circ C^{-1}]$
Alumina (α-Al ₂ O ₃)	3.984	416	257	169	8.1
Silicon carbide (α-SiC)	3.16	415	203	179	5
Yttria (Y ₂ O ₃)	5.01	158	-	-	7.9

(data from [85] for alumina, from [86] for silicon carbide and from [87,88] for yttria)

The ceramic powders from commercial sources used in the present work are presented in Table 3.2. Fine and pure α -alumina (A-16SG, ALCOA Inc., Pittsburgh, PA, USA) has been considered as the fundamental starting material. High purity and fine α -silicon carbide (Sika ABR I F1500S, Saint Gobain, Courbevoie, France) powder was chosen as the second phase to vary the thermal expansion coefficient of pure alumina. Alpha-polytype SiC was preferred to beta-polytype to avoid excessive grain growth during beta-alpha transformation [89]. Composites in the alumina/silicon carbide (AS) system with nominal composition ranging from 0 vol% to 30 vol% have been produced. In the whole text, the composites are labelled as ASxy where the first two characters represent the system AS and the last correspond to the percentage volume content of the second phase. Pure alumina (AS0) ceramic has also been produced. High purity Y₂O₃ (Yttrium oxide, Sigma Aldrich, St Louis,
MO, USA) has been chosen as liquid phase sintering additive to use in the development of pressureless sintering of alumina/silicon carbide composites. To this purpose, doped alumina composites with all the considered SiC content were also prepared by adding 2 wt% yttria and labelled as ASYxy, the first three characters representing the yttria doped AS composites.

Material	Code & producer	D50 [μm]	BET area [m²/g]	Purity [%]
Alumina (α-Al ₂ O ₃)	A-16SG Alcoa	0.4	8.6	>99.8
Silicon carbide (α-SiC)	Sika ABR I F1500S Saint-Gobain	1.8	4.9	>99.8
Yttria (Y ₂ O ₃)	Yttrium oxide Sigma Aldrich	5	5.5	99.99

Table 3.2: Ceramic powders considered in this work.

(data from products technical notes except BET area measured by BET nitrogen adsorption)

Specific surface area of the raw powders, shown in Table 3.2, was measured by BET nitrogen gas adsorption (Micromeritics ASAP 2010, Micromeritics Corp., Norcross, GA, USA). Nitrogen physisorption experiments were performed at the liquid nitrogen temperature. Samples were degassed below 1.3 Pa at 25°C prior to the analysis. Specific surface area of the samples was evaluated with the BET equation within the relative pressure range $0.05 \le p/p_0 \le 0.33$, where p_0 is the atmospheric pressure.

Crystalline phases of the powders were confirmed by X-ray diffraction investigation. The Bragg-Brentano geometry (Geiger Flex Dmax III, Rigaku Inc., Tokyo, Japan) with Cu-K_{α} radiation was used.

In addition to ceramic powders, other materials were necessary for laminates production, especially organic additives required by the forming process. As associated only to the material processing and not present in the fired ceramic, they were not included here and are discussed in the paragraph on tape casting.

3.1.2 Process selection

3.1.2.1 Green forming method

In the second chapter, several production processes to obtain ceramic laminates have been presented. Suspension processing techniques can be used to prepare green bodies with high relative density, small pore sizes and homogeneous microstructure. In the present work, tape casting has been selected as green forming technique as it is a simple and relatively low cost method which does not require any special equipment. In the past, it was successfully used to produce laminates in a variety of materials with high density and a wide range of thickness, ranging from 25 μ m up to over 1250 μ m, and is therefore suitable for the production of laminas whose thickness must be easily adjusted.

Water-based slurries were considered because of the many advantages which the universal solvent offers. Contrary to organic solvents, its use is in fact safe, healthy, low-cost and does not involve any environmental problem associated to disposal. These considerations are valid not only for the lab-scale experiments of relevance here, but mainly for any out-coming industrial application, since the volumes and the subsequent risks are extremely higher in the latter case. In addition, there are no problems related to degradation of the ceramic powders considered in this work.

The polyelectrolyte approach to produce the short-range, interparticle repulsive potential useful to obtain well dispersed slip has been chosen since it has greater applicability to many different powders and mixtures of different powders common to ceramic processing. A commercial polyelectrolyte dispersant (Table 3.3) was considered and the optimum amount obtained by literature [82,90–92]. Acrylic emulsions (Table 3.3) have been chosen as binders since they are very promising for tape casting slurry formulations owing to their features expected to reduce some drawbacks linked to aqueous preparation. The suitable amount of binder to be added has been determined experimentally, considering previous works results [22–24].

3.1.2.2 Sintering

As described in the second chapter, densification of the Al_2O_3/SiC composites is severely limited by the presence of the second phase, thus requiring hot pressing technique to achieve full densification. For many potential applications of these materials, hot pressing would be prohibitively expensive and pressureless sintering routes would be preferable if near full density could be achieved.

In this work, pressureless sintering has been chosen as one densification route to investigate the practicability of applying conventional processing to alumina/silicon carbide laminates presenting a T-curve behaviour. This would provide a basis for cost-effective scale up technique to fabricate larger amounts of near net shape products. However, as discussed in the second chapter, a significant barrier to the application of conventional sintering to alumina/silicon carbide composites is their reduced sinterability compared to alumina and their composition variations due to vaporization processes occurring at the sintering temperatures. To overcome the weight loss problem, the limitation of vapours flow in the sintering atmosphere can be used, which is achievable by enhancing the green density of the samples and reducing the size of the open porosity, or by a reduction of the sintering gas flow or by the use of a powder bed. Each one of these strategies has been selected by using a proper green forming method, realizing sintering cycles under a minimum gas flow and by surrounding the samples by a buffer bed. Even though high temperature sintering processes are generally performed in graphite furnaces, in this work an alumina tube furnace has been chosen as sintering equipment since the presence of carbon, in contact or not, in furnace environments is detrimental to alumina. In fact, formation of aluminium carbide, Al₄C₃, or oxycarbides as Al₂OC, by carbothermal reduction of alumina, starting from 1400°C, under vacuum or atmospheric pressure of argon in presence of carbon, has been reported [93,94].

The laminated Al_2O_3/SiC composites were fabricated also by means of the Spark Plasma Sintering (SPS) technique due to its beneficial characteristics. In addition, SPS had not been used before for the said kind of multilayers.

3.2 Laminates production

3.2.1 Slurry preparation

Water-based slurries to be used for tape casting have been prepared by using ammonium polymethacrylate (NH₄-PMA, Darvan C[®], R. T. Vanderbilt Inc., Norwalk, CT, USA) as dispersant and an acrylic emulsion (B-1014, DURAMAX[®], Rohm & Haas, Philadelphia, PA, USA) as binder. Similarly to previous work [23], a lower-Tg acrylic emulsion (B-1000, DURAMAX[®], Rohm & Haas, Philadelphia, PA, USA) was also added in 1:2 ratio with respect to the binder content as plasticizer in order to increase the green flexibility and reduce crack occurrence in the dried tape. Characteristics of all the organic ingredients are listed in Table 3.3.

Substance	Code & producer	Function	pН	T_g [°C]	Active matter [wt%]
NH ₄ -PMA	Darvan C® R.T. Vanderbilt, Inc.	Dispersant	7.5–9.0	-	25
High T _g acrylic emulsion	B-1014 Duramax® Rohm & Haas	Binder	3	19	45
Low T _g acrylic emulsion	B-1000 Duramax® Rohm & Haas	Plastifier	9.4	-26	55

Table 3.3: Organic ingredients used in the slurries.

Tape casting slurries have been realized by using a two-stage process [80]. An optimum dispersant content equal to 1.5 wt% with respect to the powder (about 0.4 mg/m² of active matter of Darvan C) was found in previous works [82,90–92]. The slurry was placed on ball mill in order to reach a complete dispersion. The ball milling stage, using alumina spheres of 6 mm nominal diameter, was performed in Nalgene® bottles for 24 h to break down all powder aggregates. Ball-milling was performed using a load factor (mass of alumina balls/mass of powder) equal to 1/3. 74

Then, suspensions were filtered by a 41 µm polyethylene net and de-aired using a low-vacuum Venturi pump to remove air entrapped during the milling stage. In a second stage, emulsion of acrylic binder and plasticizer were added to the obtained dispersion and slowly mixed for 30 min to reach a good homogeneity, using great care to avoid the formation of new bubbles [80]. The final organic content was 21 vol%, only the half of this values being actually organic matter (Table 3.3).

To optimize the slurry for tape casting in the case of the alumina/silicon carbide composites, a preliminary measure of the zeta potential as a function of pH, of the Sika ABR I F1500S powder was carried out in water at 25°C by using the electrophoretic light scattering technique (Delsa Nano, Zeta Potential and Submicron Particle Size Analyzer, Beckman Coulter Inc, Fullerton, CA, USA). The SiC powder exhibits negative surface electric charge in all the studied pH range (Figure 3.1) similarly to the A-16SG alumina powder dispersed with Darvan C in basic conditions (Figure 2.21). Therefore, SiC powder can be electrostatically dispersed in the alumina dispersion with no further amount of any dispersant.



Figure 3.1:Effect of pH on the zeta potential of the Sika ABR I F1500S SiC powder in water.

Hence, in the case of AS composites, silicon carbide powder was added after dispersing alumina for 24 h in the same conditions described for pure alumina and

then ball milled for additional 24 h before filtering and de-airing.

All suspensions were produced with a powder content of 39 vol%. It is useful to point out that the volume of powder in the first dispersion stage was obviously higher, equal to 50.6 vol%, since the addition of the acrylic emulsions supplies also solvent to the slurry and dilutes the slip. The recipe used to produce the composite AS30 is presented in Table 3.4 as an example. The second stage of the process for all the compositions in the AS system consisted in the addition of the emulsion binder and plasticizer and was exactly the same as for alumina. Just before casting, slurries were filtered again at 100 μ m to ensure the elimination of any bubble or cluster of flocculated polymer.

Ingredients	Function	Density [g/cm ³]	Content [wt%]	Content [vol%]	
Alumina	Ceramic	3.984	51.5	27.3	
Silicon carbide	Ceramic	3.16	18.3	11.7	
Water	Solvent	1.00	17.8	36.7	
NH ₄ -PMA	Dispersant	1.11	0.7	1.3	
High T _g acrylic emulsion	Binder	1.05	7.8	15.3	
Low T _g acrylic emulsion	Plasticizer	1.03	3.9	7.7	

Table 3.4: AS30 composite recipe.

A similar procedure was used for the preparation of composite slurries where yttria was used as sintering aid. ASY suspensions were prepared by mixing the calculated dispersant quantity and bidistilled water until the dispersant was uniformly distributed. Then the oxide used for doping, yttria, was added since basic pH is suitable for dispersing the sintering aid (Y_2O_3 dissolves extensively at low pH values [95]). After that, the alumina powder was gradually added and dispersed. The following procedure was the same as in the case of the preparation of AS composite



slurries. A flow chart of the overall production process is shown in Figure 3.2.

Figure 3.2: Flow chart of the two-stages slurry preparation process considered in this work.

3.2.2 Tape casting

Tape casting was carried out using a double doctor-blade assembly (DDB-1-6, 6" wide, Richard E. Mistler Inc., USA) at a speed of 1 m/min for a length of about 1000 mm. Such rather high translational speed was considered to obtain a minor dependence of layer green thickness on slip viscosity and speed fluctuations [80]. Also the selection of a double doctor-blade assembly was aimed to the improvement of the rheological behaviour obtained during casting, since a reduced influence of the slip level in the reservoir on the wet-tape height does exist in this case. A small lab-scale apparatus (Figure 3.3) was used to move the doctor blade with respect to the substrate (moving blade configuration).



Figure 3.3: Lab-scale apparatus used to cast slurries in the present work.

A composite three-layer film (PET12/AI7/LDPE60, BP Europack, Vicenza, Italy) was used as substrate in order to make the removal of the dried green tape easier. For this reason the polyethylene hydrophobic side of the film was placed side-up. The substrate was placed onto a rigid float glass sheet in order to ensure a flat surface and properly fixed with an adhesive tape to the borders. The relative humidity of the over-standing chamber was controlled and maintained in the range 70–80% during casting and drying to avoid a too fast evaporation of the solvent and the possible cracking of green tapes due to shrinkage stresses. For all compositions, casting of suspensions was performed using two different blade heights, 250 µm and 100 µm, to obtain different layer thickness to combine with in the laminate. In both case, either the front and the rear blade were set at the same gap height. For the sake of brevity, these two kinds of tape are labelled in the following as type I and type II

tapes, with reference to green tapes cast at 250 μ m and 100 μ m, respectively. After tape casting and drying, the green sheets showed smooth surface, homogeneous microstructure and uniform thickness of approximately 120 μ m and 50 μ m respectively.

3.2.3 Stacking and lamination

Green disks of 30 mm nominal diameter as well as sheets of nominal dimension 60 mm x 45 mm were cut from the green tapes using a hollow punch or an hand-cutter, stacked together according to the desired laminate architecture and uniaxially thermo-compressed at 80°C under a pressure of 30 MPa. The pressure was applied for 15 min in load control using a universal mechanical testing machine (mod. 810, MTS Systems GmbH, Berlin, Germany). A heating rate of about 3°C/min was considered. A 100 µm silicon-coated PET layer was placed between the laminate and the stainless steel dies to prevent sticking to steel of the surface layers and make the removal easier after thermo-compression. Care was taken to maintain the same side-up for each green lamina during pile-up to obtain a better adhesion between the different layers. In fact, it was demonstrated elsewhere that the binder distribution is not homogeneous in the green tape after drving [80.96], the bottom surface (substrate side) being richer of organic phase. Therefore, the same side was used for each lamina in a given laminate to avoid delamination. Two different kind of disks composed of 20 or 34 layers were produced: monolithic disks of identical layers and symmetrical multilayered materials constituted by a prefixed stacking of layers. For sake of brevity, these two kinds of multilayer are labelled in the following as thin (20 layers) and thick (34 layers) laminates. Only stacks of 20 laminae were used for green samples fabrication. Disks were ground with 180-grit SiC paper on the lateral surfaces to eliminate any layer misalignment or border imperfection. Bars of nominal dimensions 30 mm x 9 mm x 2 mm useful for mechanical testing were cut after thermo-compression of rectangular laminates and then re-laminated [96] before the thermal treatment to avoid any delamination caused by localized shear stresses due to cutting operations. Pre-cutting of bars is a valid solution to avoid cutting of fired laminates, since the presence of high residual stresses as well as the hardness of sintered materials make that operation a long,

tedious and low-efficient task.

3.2.4 Burn-out and pre-sintering treatment

Burn-out conditions were selected on the basis of the results of the thermogravimetric analysis on the silicon carbide powder and on the organic ingredients listed in Table 3.3. Binder, plasticizer and dispersant must be removed in fact by pyrolysis before sintering and the thermal treatment must provide for such a purpose. In addition, in order to maintain the composition in the composite materials the oxidation of the silicon carbide powder has to be avoided. Indeed, the amount of silica induced on SiC particles during processing must be carefully controlled as it results in formation of mullite and liquid phases during sintering and glassy intergranular phases in the dense materials. Thermo-gravimetric analysis of the silicon carbide powder was performed in air flow (200 cc/min) up to 1450°C at 5°C/min using a TG/DTA apparatus (STA 409, NETZSCH GmbH, Selb, Germany) to individuate the temperature range in which oxidation occurs. Thermo-gravimetric analysis of the organic ingredients was performed up to 1100°C at 5°C/min to locate the temperature range of pyrolysis phenomena and define the correct thermal treatment accordingly. An inert gas atmosphere (argon flow of 200 cm³/min) has been used to study the effect of the inert character of the atmosphere on the thermal degradation.

As time is required for polymer degradation, which occurs usually by cracking, a slow heating rate is usually required in the temperature range where pyrolysis takes place to obtain a homogeneous ceramic green. For the same reason, laminates were supported in the furnace using alumina sponges, which allow an easy removal of the produced gaseous species and lease a more uniform porosity in the ceramic body after burn-out. According to the observed pyrolysis intervals, all laminates were subjected to a debinding treatment, carried out by slow heating $(1^{\circ}C/min)$ up to 600°C in argon flow (100 cm³/min) to allow the complete burn-out of the organic phase. The temperature was then raised to 4°C/min up to 1000°C for a successive pre-sintering treatment (dwell time = 12 min) useful to produce samples that can be easily handled.

Each sample was weighed before and after the pre-sintering treatment to

determine the average weight change for the material and this was compared with the weight change detected by TG analysis to evaluate the amount of carbonaceous residue of the organic substances burn-out.

For all the AS compositions, green compact open porosity and pore size distribution were analyzed by mercury intrusion porosimetry (Pascal 140 and Porosimeter 2000, CE Instruments, Milano, Italy). The pore channel radii distribution was obtained using standard values for the mercury surface energy (484 erg/cm^2 or $4.84 \cdot 10^{-5}$ J/cm²) and the contact angle (140°).

3.2.5 Pressureless sintering

The effect of temperature, atmosphere and powder bed on pressureless sintering behaviour of alumina/silicon carbide composites, with and without yttria as sintering aid, was investigated to provide the experimental conditions found to be favourable for the laminates fabrication. Pressureless sintering of the specimens was in an alumina tube furnace (HTRH 100-300/18. GERO conducted Hochtemperaturöfen GmbH, Germany) under flowing N2 or Ar atmosphere (50cc/min) during 2h at a temperature of 1700°C or 1750°C. The heating rate was 4°C/min until high temperature. In some experiments the laminates were placed onto an alumina sponge while in other cases the samples were put in an alumina vessel and surrounded by a powder bed. Pure A16-SG alumina powder (A bed), pure Sika ABR I F1500S silicon carbide powder (S bed) and 50 mol% A16-SG/ Sika ABR I F1500S powder (AS bed) were used as beds to promote a protective atmosphere during firing. As discussed in previous chapter, sintering of Al₂O₃/SiC compositions is accompanied by the formation of volatile species as Al(g), Al₂O(g), SiO(g) and CO(g), their concentration, and consequently the weight loss in the composite, being determined by the material composition and by the sintering atmosphere and temperature. The gaseous species formation is mainly due to the interaction between an equal number of moles of Al₂O₃ and SiC (React. (2.1)). Therefore, to hinder the decomposition of SiC due to interaction with Al₂O₃, a mixture of 50 mol% of SiC and Al₂O₃ has been considered, as beneficial buffer bed, and tested. Such AS bed was produced by manually mixing the powders before the use.

After sintering, weight loss and relative density of samples were determined.

X-ray diffraction was also used to investigate the crystalline phases of selected sintered samples and the nature of the sintering residual ashes present on the alumina tube after firing. X-ray diffraction examination and density measurements were performed as described in the paragraph of the physical characterization of the homogeneous laminates.

According to the results of these investigations, the 50 mol% A16-SG/ Sika ABR I F1500S powder bed (AS bed) has been selected to promote a protective atmosphere. Argon flow (50 cm³/min) and 1750°C with an holding time of 2h have been chosen as other sintering conditions. The heating rate was 4°C/min until high temperature. A free cooling phase in the furnace followed.

3.2.6 Spark Plasma Sintering

Thin and thick pre-sintered disk-shaped laminates were subjected to spark plasma sintering. In particular, thick laminates of all AS composition from pure alumina, ASO, to AS30, were produced. Two types of thick laminate and one type of thin engineered laminates, as described in the relative paragraph, were also fabricated. Thin homogeneous alumina laminates, labelled as AS0^{III}, were also produced to compare the behaviour of the thin engineered laminate. Spark plasma sintered multilayers are labelled as AS (SPS) laminates.

Two pre-sintered samples of the same type were carefully placed into the 30 mm inner diameter graphite mould separated by a graphite spacer. The mould was then closed and placed in the SPS apparatus (Dr. Sinter 1050, Sumimoto Coal Mining Co., Tokyo, Japan). Sticking of the compacts to the punches was prevented by placing a graphite foil 200 μ m thick between the compact and the surface of punches and mould. Two laminates were sintered in each firing treatment to improve the technique productivity and to lower the fabrication costs (Figure 3.4 and Figure 3.5). The initial uniaxial pressure was equal to 6.4 MPa. A vacuum level of 10⁻² mbar was reached and a pulsed current (12 impulses of 3 ms on and two impulses of 3 ms off) was applied. The temperature was raised to 600°C in 5 min and then monitored and regulated by means of an optical pyrometer.



Figure 3.4: Schematic representation of the SPS configuration adopted in the present work.



Figure 3.5: Photograph showing the elements constituting the core of the SPS ensemble. From the left, a graphite punch, a graphite die, a laminate sample, a graphite spacer, a laminate sample and a graphite punch are recognizable.

Then, the uniaxial pressure was raised to 28.7 MPa and the temperature was increased, at first up to 1650° C (heating rate = 100° C/min) and then to 1700° C (heating rate = 50° C/min). After a holding time of 2 min, the pressure was released, the current turned off, and the sample cooled down. A sintering temperature equal to 1700° C was chosen for the spark plasma sintering process to obtain dense microstructures for all the compositions and to make a comparison with the analogous pressureless sintered materials.

3.3 Homogeneous Laminates

3.3.1 Physical characterization

Crystalline phases in selected sintered samples were examined through Xray diffraction in the Bragg-Brentano geometry (Geiger Flex Dmax III, Rigaku Inc., Tokyo, Japan) with Cu-K_a radiation, operated at 40 kV and 30 mA, and a graphite monochromator in the diffracted beam. The step size and step time are 0.05° /step and 5 s respectively. The quantity of phase composition of selected samples was analyzed with Rietveld refinement of the XRD data. The Rietveld analysis program Materials Analysis using Diffraction (MAUD, Version 2.26) [97] was employed to evaluate the collected diffraction patterns.

Bulk densities of sintered samples were measured by the Archimedes' immersion method in de-ionized water at room temperature. Six samples for each material were considered. Relative densities and porosity were also calculated with reference to the theoretical densities of fully densified composites. Assuming a density of 3.984 g/cm^3 for alumina and 3.16 g/cm^3 for silicon carbide (Table 3.1), the theoretical densities of composites were calculated by the rule of mixtures:

$$\rho_{12} = \rho_1 f_{v1} + \rho_2 (1 - f_{v1}) \qquad \qquad Eq. (3.1)$$

where ρ_{12} , ρ_1 and ρ_2 are the densities of the composite, phase 1 and phase 2 respectively and f_{v1} the volume fraction of phase 1.

The thermal expansion coefficient required for the residual stress calculation by Eq. (2.15) and Eq. (2.16) was measured in the range 25–1000°C by a dilatometry 84 apparatus (DIL 402, NETZSCH GmbH, Selb, Germany) using an alumina sample holder and a heating rate of 5°C/min. The experimental values were compared to the Turner's equation [3] proposed to estimate the thermal expansion coefficient of a generic composite with a fine and equiaxed microstructure, reported in the following in the case of a two phase composite:

where B_1 and B_2 are the bulk moduli of phase 1 and 2, respectively, α_1 and α_2 the corresponding thermal expansion coefficients and f_{v1} the volume fraction of phase 1.

The microstructure of the sintered materials was observed using Scanning Electron Microscopy, SEM, (JSM-5500, JEOL Inc., Tokyo, Japan) and energy dispersive microanalysis (Analyzer 500, IXRF Systems Inc., Houston, TX, USA). Specimen surfaces were polished to 1 µm and thermally etched at 1500°C for 20 minutes in argon atmosphere. The average grain size, G, of monolithic alumina samples was evaluated on SEM micrograph using the lineal intercept technique:

$$G = 1.56 \frac{C}{MN} \qquad \qquad Eq. (3.3)$$

where C is the total length of test line used, N the number of intercepts and M the magnification of the photomicrograph [98]. A modified lineal intercept equation was used to obtain the average grain size of the primary phase in two phase systems:

$$G = 1.56 \frac{C_{\text{eff}}}{MN_{\text{eff}}} \qquad Eq. (3.4)$$

where C_{eff} is the corrected test line length and N_{eff} the effective number of intercept [99]. Randomly drawn lines intersecting at least 150 grains was considered for each measure. Silicon carbide grains were identified by energy dispersive microanalysis and generally appeared smooth and light coloured relative to alumina. The 85

observation of fracture surface of homogeneous and engineered laminates after mechanical testing was also done by SEM.

3.3.2 Mechanical characterization

The spark plasma sintered compact disks were ground with 250 μ m diamond wheel on the lateral surface to facilitate the graphite foil removal and cut with a diamond blade into rectangular bars (thin and thick laminates to approximately 1.3 x 7 x 25 mm and 2 x 7 x 25 mm, respectively). Pressureless sintered bars with approximately 1.7 x 7 x 25 mm nominal dimensions were produced. Each laminate was ground using 125 μ m grain size diamond disk to obtain lateral surfaces perpendicular to the laminas plane. The edges, to be in tension, of specimens were bevelled with 800-grit SiC paper to remove macroscopic defects and geometric irregularities. In the case of spark plasma sintered samples, the provisional tensile load surface of all bend specimens was the one in contact with the graphite punch and perpendicular to the pressing axis. No further polishing or finishing operations were performed on the sample surfaces or edges to avoid any artificial reduction of flaws severity.

Fracture strength test was carried out in four-point bending mode with inner and outer span of 10 and 20 mm, respectively, with crosshead speed of 0.2 mm/min. The tests were performed according to the ASTM Standard C 1161-02c, though the samples did not conform to the exact size recommendations. The strength values were calculated from the average of 10-12 tests at each load.

Young's modulus, E, was calculated from the load-displacement curve obtained by four-point bending test. All displacement data were corrected for the machine stiffness. Assuming a Young' modulus of 416 GPa for alumina and 415 GPa for silicon carbide (Table 3.1), the theoretical Young's modulus of fully densified composites was considered to remains quite unvaried according to the Hashin-Shtrikman model and the equation:

$$E = \frac{9\mu B}{3B + \mu} \qquad \qquad Eq. (3.5)$$

where B and μ are the bulk modulus and the shear modulus determined as an average of the upper and lower bounds calculated according to the model. In the case of porous pressureless sintered materials the equation proposed by Roberts and Garboczi [100] was used to estimate the elastic modulus:

where E is the Young's modulus of the porous material, P is the porosity, E_0 is the Young's modulus of the dense material, P_0 and n are empirical correlation parameters depending on the pores model.

The Poisson's ratio of the spark plasma sintered homogeneous laminates were also calculated by Hashin-Sthtrikman model and the equation:

$$v = \frac{3B - 2\mu}{2(3B + \mu)} \qquad Eq. (3.7)$$

where B and μ are the bulk modulus and the shear modulus determined as an average of the upper and lower bounds calculated according to the model. In the case of porous pressureless sintered materials the equation proposed by Roberts and Garboczi [100] was used to estimate Poisson's ratio:

$$v = v_0 + \frac{P}{P_0} (v_n - v_0) \qquad \qquad Eq. (3.8)$$

where v is the Poisson's ratio of the porous material, P is the porosity, v_0 is the Poisson's ratio of the dense material, P_0 and v_n are fitting parameters depending on the pores model.

The hardness, H, values were measured by means of Vickers indentation method from the following formula [6]:

$$H = 1.8544 \frac{P}{d^2}$$
 Eq. (3.9)

where P is the indentation load and d the projected diagonal of the indentation. A load of 300 N was applied for 15 s on the 1 μ m polished surface perpendicular to the pressing axis, in the case SPS laminates.

Fracture toughness, K_{IC} , was calculated using the Indentation Method (IM)[101] after measuring the radial crack length, c, by optical microscopy using a 200X magnification:

$$K_{IC} = 0.016 \left(\frac{E}{H}\right)^{0.5} \frac{P}{c^{1.5}}$$
 Eq. (3.10)

sintered pressureless sintered alumina Spark plasma and (AS0) homogeneous additional laminates were also subjected to mechanical characterisation, including a Weibull analysis, tests of post-indentation strength and a fractographic analysis of broken samples, as described in detail in the following paragraph. Only this composition was considered in these analyses since alumina is the proper reference material to make a mechanical behaviour comparison respect to the engineered laminates. Indeed, alumina represents the ceramic constituting the internal region and the surface layer of the engineered multilayers.

3.4 Engineered Laminates

3.4.1 Structure of engineered laminates

In the second chapter an approach to design laminates with high mechanical reliability has been presented. Considering the selected composite materials, the two layers thickness (types I and II) cast in the present work and the two sintering methods (PS and SPS), five different multilayered symmetric laminates were designed and produced. The structure of the laminates was selected to obtain a residual stress profile optimised to support bending loads and promote a stable propagation of surface defects up to a maximum depth in the interval 50–85 µm. Such laminates, labelled as AS-I (PS), ASY-I (PS) and AS-I (SPS), AS-II (SPS), AS-III (SPS) present the structures shown in Figure 3.6. AS-I (PS) was produced by pressureless sintering using composites in the sole AS system, ASY-I using also yttria as sintering aid, whereas AS-I (SPS), AS-II (SPS), AS-III (SPS) were obtained 88

by spark plasma sintering of AS composites multilayers in order to obtain fully densified materials. If a notation similar to that used for composite plies is considered [11], the multilayer structure in terms of composition and sequence of the laminae can be expressed as:

AS-I (PS)	$AS0_{II}/AS10_{II}/AS20_{II}/AS10_{II}/(AS0_{I})^{16}//$
ASY-I (PS)	$AS0_{II}/ASY10_{II}/ASY20_{II}/ASY10_{II}/(AS0_{I})^{16}//$
AS-I (SPS)	$AS0_{II}/AS10_{II}/AS20_{II}/AS10_{II}/(AS0_{I})^{30}//$
AS-II (SPS)	$AS0_{II}/AS20_{II}/AS30_{II}/AS20_{II}/(AS0_{I})^{30}//$
AS-III (SPS)	AS0 _{II} /AS10 _{II} /AS20 _{II} /AS10 _{II} /(AS0 _I) ¹⁶ //

where the numerical subscripts represent the layer type previously discussed (I = type I, II = type II) and the superscript represents the times a single layer is repeated. In this notation the symbol slash ("/") separates two contiguous layer and, if repeated twice, represents the symmetry plane at the centre of the laminate. As usually, the sequence presented above starts from the external layer. For instance, the laminate AS-III (PS) is obtained by spark plasma sintering stacks of, in the order, one thin AS0 layer, one thin AS10 layer, one thin AS20 layer, one thin AS10 layer and finally sixteen thick AS0 layers. Such sequence is repeated in the reverse order in order to obtain a symmetric multilayer (Figure 3.6). Typical layers thickness, as estimated on the produced engineered laminates by optical microscopy and SEM, are also reported in Figure 3.6.

The residual stress distributions were calculated for each laminate by Eq. (2.15) and the corresponding T-curve estimated according to the model represented by Eq. (2.17) using a numerical procedure implemented in a commercial software (MATHEMATICA®, Wolfram Research, Inc., Champaing, IL, USA), the code being listed in the Appendix.



Figure 3.6: Schematic representation of the symmetric laminates structures considered in this work. Layers thicknesses and compositions are reported. Dimensions are not in scale.

To this purpose, the required material properties, as Young modulus, thermal expansion coefficient and fracture toughness, as well as the layer thickness estimated by previous characterisation were used. The free deformation was supposed to be related only to thermal expansion and room temperature of 25°C and stress free temperature equal to 1200°C were considered in Eq. (2.15) according to previous works [62]. Once the correct trend of the T-curve was numerically estimated, the design bending strength and threshold stress were estimated by Eq. (2.19) and Eq. (2.20), as well as the depth of the largest edge cracks propagating in a stable fashion.

3.4.2 Weibull analysis and post-indentation strength

Sintered bars of the engineered laminates AS-I (PS), ASY-I (PS), AS-I (SPS), AS-II (SPS), AS-III (SPS) together with the corresponding homogeneous alumina laminates AS0 (PS), AS0 (SPS), $AS0^{III}$ (SPS) with 7 mm x 25 mm nominal dimension were ground using a 125 μ m grain size diamond disk to obtain lateral surfaces perpendicular to the laminas plane. Edges were slightly chamfered with 800 SiC papers to remove macroscopic defects and geometrical irregularities as previously described.

Four-points bending tests were carried out using the same apparatus described before with an actuator speed of 0.2 mm/min and inner and outer span of 10 mm and 20 mm, respectively. For each laminate, 26–30 samples were considered, while 12–20 samples were tested in the case of thick spark plasma sintered laminates. A Weibull analysis was performed on bending strength data. Monolithic alumina specimens produced using the same sintering conditions were tested for comparative purposes.

Using the same experimental apparatus and the same test conditions, bending strengths on indented samples were also measured in order to investigate the damage tolerance of the engineered laminates. Vickers indentations with loads of 10 N, 30 N and 100 N were placed on the sample surface to introduce defects of different sizes. Three indentations were produced in the centre of the perspective tensile surface. Homogeneous AS0 (PS), AS0 (SPS) and AS0^{III} (SPS) were also tested in the same conditions for comparison. For each condition 3–4 indented

samples were considered, while only two samples of the AS-II (SPS) laminate, indented at 30 N and 100 N, were tested. In the case of pressureless sintered engineered laminates, some indentations at higher loads (150 N) were also performed to investigate the interaction of deeper cracks with the sub-surface residual stress profile.

The mechanical behaviour observed in the case of the five optimised multilayers considered in the present work is presented in the next chapter. As previously discussed, the mechanical behaviour of each profile is compared to that one of the corresponding homogeneous laminate.

3.4.3 Investigation on stable growth

The reduced strength scatter expected for the optimised laminates is related to the T-curve behaviour promoted by the residual stress profile. In addition to an increase of damage resistance, stable growth phenomena for surface cracks are expected to occur. An experimental verification of such a stable propagation of surface cracks is therefore aimed to prove that what designed actually happens. Fractographic analysis is an important tool to understand the fracture mechanisms, allowing to identify whether the fracture was a result of material deficiency or residual stress induced condition by design.

A fractographic analysis of the fracture surfaces of indented and nonindented broken samples was performed either for the engineered and the corresponding homogeneous laminates. The fracture origin and location, on surface or near surface, was identified. The presence of any mark or unexpected feature was recorded, paying special attention to the presence of the fracture mirror, when present. Both optical and scanning electron microscopy were used to this purpose.

As already discussed in the second chapter, when the critical condition for brittle failure is reached (Eq. (2.2)), crack starts to propagate increasing its speed up to a maximum value. Beyond this point, any further mechanical energy released is dissipated by crack tilting, twisting and branching and the fracture surface presents a higher roughness. Therefore, a smooth region is usually present just near the starting defect while roughness increases at larger distance (Figure 2.4). In most cases, two kinds of region can be typically recognised: a mist zone with a medium roughness 92

and a hackle zone where roughness is coarser. This special feature is always produced on the fracture surface around the crack origin, its shape being associated to the loading condition and its size to the strength value [29]. Nevertheless, it is important to point out that if no mirror is observed on the surface, there is also the possibility that this is associated to a low fracture strength, since the radius of fracture mirror can be larger than the sample section.

Regardless the actual size of the fracture mirror, its shape is expected to give useful information about the position of the starting defect and to the loading condition, the negative curvature pointing the direction of crack propagation and the opposite showing therefore the side where crack origin is. The position and shape of the fracture mirrors observed for the engineered laminates and for the corresponding homogeneous samples were discussed to investigate the kind of the critical defects.

Chapter IV

Results and discussion

4.1 Green tapes

Flexible and homogeneous green tapes were successfully obtained (Figure 4.1). The quality of the produced green tapes and the validity of the overall process was verified either by the ease of cutting as well as by the perfect adhesion observed between layers after thermo-compression. After sintering, in fact, no marks at the interface were observed in the homogeneous laminates and defect-free dense monolithic materials were produced.



Figure 4.1: AS30 green tape (type I) produced in this work. Coiled and twisted green ribbons are shown to emphasize green resistance and flexibility. The ease of peeling of the tape from the substrate is also shown.

Also the peeling action of the dried green tape from the substrate was an easy task (Figure 4.1), even in the case of thinner tapes. This is a further evidence of the quality of the green material since a certain mechanical resistance is required for safe peeling. No defects were observed in the green tapes during the preliminary analysis.

The thickness of type I and type II tapes was measured using a high precision digital micrometer. Type I green tapes showed a dried thickness of about 120 μ m, not depending on slip composition and close to half of the considered blade gap (250 μ m). Type II green tapes showed a dried thickness in the range 50 μ m, again close to the half of the considered blade gap (100 μ m). A clear reduction of green thickness is due to the lamination process, its average effect estimated in about 6% for a single thermo-compression and 11.5% for a twice-repeated operation.

4.2 **Pre-sintered laminates**

Since the selected silicon carbide powder undergoes to oxidation in air also at low temperatures (Figure 4.2), argon as inert atmosphere has been chosen for the pyrolysis treatment.



Figure 4.2: Thermogravimetric analysis of the silicon carbide powder in air. Weight gain, due to the carbide oxidation, is shown also at low temperatures.

From the TG curves in argon flow of the three organic ingredients (Figure 4.3) it can be observed that weight loss takes place mainly in the range between 200°C and 500°C for the dispersant and close to 400°C for the other substances. Quite a complete decomposition is achieved in only one stage for binder and plasticizer. From it can be appreciated that the residue after pyrolysis is not zero for all materials. An amount of carbonaceous residue equal to 7.5–13.5 wt% is present after the thermal treatment.



Figure 4.3: Thermogravimetric analysis of the organic ingredients in argon. Weight loss due to polymer degradation takes place mainly in the range 200–500°C.

Black, resistant and easy-to-handle samples were obtained after the presintering treatment. Incomplete binder born-out was supposed, based on the colour of the samples, on the results of calculated (as complete burn-out) and measured weight loss (Figure 4.4) after the thermal cycle and on the thermogravimetric analyses performed on the organic binders. In fact, when organic binders are pyrolyzed in oxygen free atmosphere it can inherently memorize their dangling structure. This lead to a long range interconnection of pyrolyzed carbon which is continuously and uniformly distributed throughout the ceramic microstructure. Normally, the concentration of pyrolyzed carbon derived from polymer is minimal but enough to change the entire colour of the sample to black. The residual carbonaceous matter in the pre-sintered laminates, estimated as equal to 5.5 ± 0.7 wt%, was considered acceptable since no adverse effect was supposed to occur in the following sintering step. Indeed, graphite contamination from the mould is expected anyway to happen in spark plasma sintering, while no densification limits are supposed to be encountered in the presence of such a small amount of carbon, in pressureless sintering.



Figure 4.4: Weight loss of the alumina/silicon carbide composites, calculated and measured after burn-out in Ar atmosphere, as a function of SiC content.

 Table 4.1: Average pore radius and relative density of the pre-sintered alumina/silicon carbide composites.

	SiC content [vol%]						
	0	5	10	15	20	25	30
Average pore radius [nm]	63	77	67	77	93	90	91
Relative density [%]	57.2	52.8	53.5	54.8	53.0	53.6	55.4

The pre-sintered monolithic laminates exhibited a total porosity of approximately 45% (Table 4.1) with narrow pore size distribution from 63 nm to 93 nm. The packing density and quality of green samples is high enough to help the sintering of the compacts. The addition of yttria had no significant effect on the green properties and on the pore size distribution of the alumina compacts.

Frequent delamination was encountered during the pre-sintering process of the AS-II (SPS) laminate samples where layers containing large compressive stresses (AS30) are present. The high residual stresses produced by thermal mismatch upon cooling can not be sustained, in fact, by the porous green materials and shear delamination occurs. Nevertheless, this result can be considered as a proof of the existence of high residual stresses directly related to the sole contribution of thermal expansion mismatch.

4.3 Pressureless sintering

The pressureless sintered Al₂O₃/SiC compacts exhibited weight loss in the order of 1–6 wt% (Figure 4.6) at 1700°C, the higher values corresponding to higher SiC content and for the samples sintered on the alumina sponge. The use of an Ar atmosphere and of the AS bed led to the lower weight loss, equal to about 1 wt% for all compositions (Table 4.2). Relative densities decreased with SiC content, ranging from about 90% for pure alumina to about 65% for the AS30 composite (Figure 4.7 and Table 4.2). When N₂ was used as sintering atmosphere a better densification of alumina was achieved respect to Ar, as observed by Coble [102]. Indeed, N₂ provide less resistance to final pore closure in alumina due to a higher diffusivity. However, the effect of N₂ in the sintering of the composites was detrimental, especially for high SiC contents (Figure 4.6 and Figure 4.7).

Weight losses were increased at 1750°C, reaching values of about 16% when N_2 was used as sintering gas (Figure 4.8). Mass changes were higher for samples placed on alumina sponge or into alumina bed, and were minimized (~1–2.5 wt%) in the case of the AS bed, as expected by considering the vaporization reaction occurring in the firing treatment. Relative densities were slightly increased respect to the 1700°C firing cycle (Figure 4.9 and Table 4.2).

Analogous considerations could be proposed when yttria was used as

sintering aid. Increasing temperature led to higher weight losses, particularly for higher SiC content and when a certain amount of SiC was not surrounding the samples. The use of the AS bed reduced the mass change that remained as equal to ~1 wt% at 1700°C and ~1–2.5 wt% at 1750°C (Figure 4.10–Figure 4.13 and Table 4.2). Densification of the composites was increased respect to the non doped materials, especially at 1750°C, and limited to ~70% for the AS30 laminate (Table 4.2). From Table 4.2, it can be also seen that densification of yttria doped composites was improved at 1750°C, which is similar to the melting point of yttrium aluminum garnet (YAG), suggesting that it is the formation of a YAG liquid phase which allows sintering to occur [103].

X-ray patterns of residual ashes (Figure 4.5) present on the alumina tube after firing tests conducted at 1750°C in Ar support the identification of silicon (ICDD File Card Number 27-1402) as main constituent. This result suggest the formation of Si by the reaction of gaseous SiO with small amount of C, present in the samples, as carbonaceous residue, and in the firing atmosphere, validating React. (2.1).



Figure 4.5: Residual ashes formed into the furnace alumina tube during alumina/silicon carbide composites sintering.



Figure 4.6: Weight loss as a function of SiC content after sintering of Al₂O₃/SiC composites at 1700°C.



Figure 4.7: Relative density as a function of SiC content after sintering of Al₂O₃/SiC composites at 1700°C.



Figure 4.8: Weight loss as a function of SiC content after sintering of Al₂O₃/SiC composites at 1750°C.



Figure 4.9: Relative density as a function of SiC content after sintering of Al₂O₃/SiC composites at 1750°C.



Figure 4.10: Weight loss as a function of SiC content after sintering of Y_2O_3 -doped Al₂O₃/SiC composites at 1700°C.



Figure 4.11: Relative density as a function of SiC content after sintering of Y₂O₃doped Al₂O₃/SiC composites at 1700°C.



Figure 4.12: Weight loss as a function of SiC content after sintering of Y_2O_3 -doped Al₂O₃/SiC composites at 1750°C.



Figure 4.13: Relative density as a function of SiC content after sintering of Y₂O₃doped Al₂O₃/SiC composites at 1750°C.

	1700°	1700°C		1750°C		
laminate	wt loss [%]	ρ_{rel} [%]	wt loss [%]	ρ _{rel} [%]		
AS (PS) compo	osites					
0	0.99	91.8	1.02	93.8		
5	1.14	89.3	1.40	90.6		
10	1.32	81.4	1.78	82.3		
15	1.44	73.4	1.68	72.9		
20	1.15	67.9	2.07	68.2		
25	1.16	65.7	2.58	65.9		
30	1.07	65.0	1.78	64.0		
ASY (PS) comp	posites					
0	1.26	93.7	1.12	95.4		
5	1.51	89.9	1.08	94.6		
10	1.49	82.6	1.75	91.9		
15	1.12	73.5	2.15	87.5		
20	1.04	67.2	2.71	74.8		
25	0.95	65.5	2.30	73.4		
30	1.07	63.7	2.45	70.1		

Table 4.2: Weight loss (wt loss) and relative density (ρ_{rel}) of alumina/silicon carbide composites, with or without yttria as sintering aid, after sintering surrounded by the AS bed.

The AS composites sintered at 1750°C in Ar exhibited the presence of only α -Al₂O₃ (ICDD File Card Number 10-173) and α -SiC (ICDD File Card Number 29-1131). No presence of oxycarbides, carbide, or mullite was observed. When yttria was used as sintering aid, YAG (ICDD File Card Number 88-2048) was found in the samples. The composition of the AS20 composite surrounded by AS bed and sintered at 1750°C in Ar atmosphere was confirmed by Rietveld refinement.

All these results confirm the validity of the processing and are consistent

with the view that the effect of the powder bed is to limit the escape from the sample of any volatile components, which might have formed during heating, by surrounding it with an equivalent partial pressure of the volatile species in the powder bed and minimizing the driving force for diffusion out of the sample.

4.4 Spark plasma sintering

Fully dense and thin compacts can be obtained by spark plasma sintering at temperatures ranging from 1335°C for pure alumina to 1475°C for the AS30 (SPS) composite (Figure 4.14) as observed by the recorded displacement rate versus temperature diagram of the powder compacts.

The use of graphite foil between the compact and the surface of punches and mould in the SPS apparatus is mandatory to prevent sample bonding to the punches and its subsequent rupture due to different contraction during cooling down (Figure 4.15). A graphite spray is not sufficient for this purpose, although it allows a better surface finishing.



Figure 4.14: Spark Plasma Sintering temperature of the AS composites, observed in this work, as a function of SiC content.


Figure 4.15: Photograph showing laminate rupture due to sample bonding to graphite punches, when graphite spray was used as releasing agent. Intact sample (right) was produced by wrapping in graphite foils.

4.5 Homogeneous laminates

4.5.1 Microstructure and composition

Figure 4.16 shows a SEM image showing the typical microstructure of the AS0 (SPS) homogeneous laminate. Polishing and thermal etching at 1500°C for 20 min was used to highlight the grain boundaries. Microstructure is dense and quite homogeneous. No preferred orientation can be observed in the grains. As shown in Table 4.3, an average grain size of $2.4 \pm 0.2 \mu m$ was calculated by Eq. (3.3). This demonstrates that no important grain coarsening occurred, also when high firing temperature (1700°C) are used, it being a direct consequence of the spark plasma sintering technique. The appearance of the pressureless sintered alumina AS0 (PS) (Figure 4.17) was similar to the spark plasma sintered material with a larger grain size, equal to $5.6 \pm 0.5 \mu m$. Grain coarsening is due to the high temperature, 1750°C, used in pressureless sintering. X-ray patterns of the pure alumina samples, produced by both spark plasma sintering and pressureless sintering, support the identification of only α -Al₂O₃ (ICDD File Card Number 10-173) and confirm the material composition.

The typical microstructure observed in the case of AS (SPS) composites is shown in Figure 4.18 for the AS30 composite. The smooth sharp gray grains represent the silicon carbide phase while the regular grains correspond to alumina. The colour contrast between the two phases is not intense due to the low mismatch between the element mass present in alumina and silicon carbide. Phases are homogeneously and randomly distributed, this being a proof of the optimum slurries preparation. No pores or cracks are present and a fully-dense microstructure is obtained. Alumina grain size is smaller than in pure alumina (Table 4.3), and no large grains are present at all. This fact corresponds to the expected retaining effect of silicon carbide grains on the alumina grain growth. From the values presented in Table 4.3 for some selected composites, it can be appreciated that the effect increases with the silicon carbide content, a value as small as $1.4 \pm 0.1 \,\mu$ m being recorded for the AS30 composite. Silicon carbide grains remain quite large, presenting a micrometric average grain size equal to about 4.2 μ m for all the compositions.

Figure 4.19 presents a SEM image of the AS20 (PS) composite. Differently from the AS (SPS) composites, a significant residual porosity can be noticed. The residual porosity and the incomplete sintering observable in the pressureless sintered homogeneous composites are due to the detrimental effect of SiC on alumina sintering, as already discussed in the second chapter. The spark plasma sintered and pressureless sintered AS composites exhibited the presence of only α -Al₂O₃ (ICDD File Card Number 10-173) and α -SiC (ICDD File Card Number 29-1131), the composition of the AS20 (PS) composite being confirmed by Rietveld refinement. No presence of oxycarbides, carbide, or mullite was observed.

Figure 4.20 shows the typical microstructure of yttria doped alumina ASY0 (PS). Microstructure is dense and quite homogeneous with equiaxed gray alumina grains with an average size of $4.5 \pm 1.0 \mu m$ (Table 4.3). Therefore, no increase of alumina grain size related to the presence of yttria was observed. Small regions of a white phase assumed to be yttrium aluminum garnet (YAG) situated within the alumina grains are clearly visible in Figure 4.20.



Figure 4.16: SEM image of the typical microstructure observed in ASO (SPS).



Figure 4.17: SEM image of the typical microstructure observed in ASO (PS).



Figure 4.18: SEM image of the microstructure observed in AS30 (SPS).



Figure 4.19: SEM image of the typical microstructure observed in AS20 (PS) composite.



Figure 4.20: SEM image of the microstructure observed in the ASY0 (PS) material.

Table 4.3: Grain sizes of alumina (G_A) and silicon carbide (G_S) mea	isured in
selected homogeneous composites.	

laminate	$G_A \left[\mu m \right]$	$G_S \left[\mu m \right]$
AS (PS) composites		
ASO (PS)	5.6 ± 0.5	-
ASY (PS) composites		
ASY0 (PS)	4.5 ± 1.0	-
AS (SPS) composites		
AS0 (SPS)	2.4 ± 0.2	-
AS20 (SPS)	2.0 ± 0.2	4.2 ± 2.1
AS30 (SPS)	1.4 ± 0.1	4.1 ± 2.3

Similarly to the AS (PS) composites, a significant residual porosity was also observed in the ASY (PS) composites. The formation of intergranular YAG (ICDD

File Card Number 88-2048) was confirmed by EDX analysis showing the presence of yttria in the white regions and by XRD investigation on the ASY (PS) samples, as discussed in the previous chapter.

4.5.2 Density and porosity

Density (Figure 4.21) and porosity results as obtained by Archimedes' principle are presented in Table 4.4 for all the compositions. For each composite relative density with respect to the theoretical value for the given composite estimated by Eq. (3.1), which represents simply the rule of mixtures of a two-phase composite is also shown.



Figure 4.21: Density as a function of SiC content in the monolithic laminates considered in this work. Calculated theoretical density (Th) is also shown for comparison.

In excellent agreement with the qualitative considerations presented on the basis of the SEM microstructures, AS (SPS) composites show a dense structure, the relative density being in every case larger than 96.1%. Pure alumina AS0 (SPS) is fully densified and presents a fired density of 3.92 g/cm³, corresponding to 98.4%. Conversely, pressureless sintered laminates, with or without yttria, present a residual porosity, whose value increases strongly with the SiC content, up to a value as high

as 24.8% for the ASY20 (PS) composition and even 34.9% for the AS20 (PS) composite. Due to the high porosity values of the composites exceeding the 20 vol% SiC content, only AS (PS) and ASY (PS) composites with up to this composition have been considered as usable for engineered laminates fabrication, and hence investigated. The pressureless sintered alumina, with or without yttria added, reach a relative density as equal to 93% and 95.3% respectively.

laminate	$\rho [g/cm^3]$	$ ho_{rel}$ [%]	P [%]
AS (PS) composites			
0	3.70 ± 0.03	93.0 ± 0.8	0.8 ± 0.7
5	3.48 ± 0.03	88.3 ± 0.8	6.0 ± 0.9
10	3.05 ± 0.02	78.2 ± 0.6	21.0 ± 0.7
15	2.77 ± 0.07	71.6 ± 1.7	27.5 ± 1.2
20	2.47 ± 0.11	64.8 ± 2.9	34.9 ± 2.9
ASY (PS) composites			
0	3.81 ± 0.01	95.3 ± 0.4	0.1 ± 0.1
5	3.80 ± 0.01	96.0 ± 0.4	0.7 ± 0.2
10	3.57 ± 0.06	91.0 ± 1.5	5.7 ± 1.9
15	3.41 ± 0.06	87.9 ± 1.5	12.8 ± 1.0
20	2.94 ± 0.05	76.7 ± 1.3	24.8 ± 0.9
AS (SPS) composites			
0	3.92 ± 0.02	98.4 ± 0.5	0.5 ± 0.3
5	3.89 ± 0.01	98.7 ± 0.2	0.7 ± 0.3
10	3.85 ± 0.01	98.8 ± 0.3	0.2 ± 0.2
15	3.80 ± 0.02	98.5 ± 0.5	0.5 ± 0.2
20	3.75 ± 0.02	98.2 ± 0.4	0.3 ± 0.2
25	3.65 ± 0.01	95.8 ± 1.1	1.7 ± 0.6
30	3.59 ± 0.02	96.1 ± 0.6	1.8 ± 0.3

Table 4.4: Density (ρ), relative density (ρ_{rel}) and porosity (P) as measured by Archimedes' principles on the AS composites.

The reasons of the differences between the spark plasma sintered and the pressureless sintered composites were already partially discussed in previous chapters. Indeed, diffusion at the Al₂O₃/SiC interface is slower than at the Al₂O₃/Al₂O₃ interface due to the strong directional bonding of both Al₂O₃ and SiC. Since densification in alumina is controlled by grain boundary diffusion the presence of intergranular SiC limits densification [42]. Particularly, alumina/silicon carbide composites are usually produced by using pressure aided processes to obtain dense bodies [11,26]. The presence of yttria as sintering aid in the ASY (PS) laminates is beneficial as the relative density of the composites is increased for all the compositions.

4.5.3 Thermal expansion behaviour

The thermal expansion coefficients measured by using an alumina sample holder and averaged in the temperature range 25–1000°C are presented in Table 4.5 for all the compositions considered in the present work. The AS laminates show a lower thermal expansion than pure alumina (AS0), the decrease being a direct function of silicon carbide content (Figure 4.22).



Figure 4.22: Thermal expansion coefficients of the AS composites sintered by SPS as a function of SiC content. Theoretical trend estimated by Turner's equation is also shown (dashed line).

laminate	E [GPa]	ν	H [GPa]	K _{IC} [MPa m ^{0.5}]	α [10 ⁻⁶ °C ⁻¹]
AS (PS) composites					
0	389 ± 46	0.230	15.8 ± 0.4	2.9 ± 0.2	8.80
5	388 ± 7	0.227	12.2 ± 0.7	3.1 ± 0.2	8.59
10	306 ± 26	0.223	6.1 ± 0.1	3.5 ± 0.3	8.57
15	230 ± 14	0.220	3.8 ± 0.1	3.2 ± 0.2	8.39
20	139 ± 22	0.219	1.8 ± 0.1	2.9 ± 0.1	8.27
ASY (PS) composites					
0	396 ± 22	0.230	15.3 ± 1.0	2.9 ± 0.2	8.82
5	386 ± 21	0.227	12.0 ± 0.1	3.2 ± 0.2	8.63
10	353 ± 22	0.224	5.7 ± 0.1	3.5 ± 0.4	8.47
15	284 ± 37	0.220	3.6 ± 0.4	3.2 ± 0.4	8.30
20	193 ± 13	0.218	2.1 ± 0.1	3.0 ± 0.3	8.18
AS (SPS) composites					
0	398 ± 31	0.230	17.0 ± 1.4	3.0 ± 0.3	8.80
5	398 ± 14	0.227	17.1 ± 0.7	3.1 ± 0.4	8.52
10	394 ± 38	0.224	17.5 ± 0.8	3.3 ± 0.1	8.45
15	397 ± 28	0.220	16.7 ± 0.8	3.4 ± 0.1	8.35
20	366 ± 9	0.217	17.2 ± 1.1	3.3 ± 0.2	8.03
25	400 ± 22	0.214	16.1 ± 0.4	3.5 ± 0.1	7.99
30	382 ± 53	0.210	16.2 ± 0.5	3.3 ± 0.1	7.87

Table 4.5: Young modulus (E), Poisson's ratio (v), hardness (H), fracture toughness (K_{IC}) and average thermal expansion coefficient (α) of the homogeneous laminates considered in this work.

This is exactly what one could expect on the basis of the expansion behaviour of alumina and silicon carbide assumed as equal to $8.8 \cdot 10^{-6} \text{ °C}^{-1}$ and $5 \cdot 10^{-6} \text{ °C}^{-1}$ respectively. AS0 presents an average coefficient of $8.8 \cdot 10^{-6} \text{ °C}^{-1}$ and AS composites

lower values down to $7.9 \cdot 10^{-6} \, {}^{\circ}C^{-1}$ (AS30). The data of the AS (SPS) laminates are plotted in Figure 4.22 and compared to the theoretical coefficients estimated by Turner's equation (Eq. (3.2)). Very close agreement exists between the trend shown by expected and experimental data. In addition, since the presence of porosity in the material is not expected to influence the thermal expansion behaviour [6] no significant differences in the thermal expansion coefficients between the spark plasma sintered laminates and the corresponding porous pressureless sintered materials were observed. Therefore, the actual thermal expansion coefficients are in good agreement with respect to common literature data and this confirms the goodness and the reliability of the processing procedure used in the present work. Finally, it is possible to point out that the thermal behaviour in the AS composite system was tailored successfully by adjusting the composition and a good range of thermal expansion coefficients was available for laminates design.

4.5.4 Young's modulus and Poisson's ratio

Table 4.5 presents also the values of Young's modulus measured on the homogeneous laminates considered in this work. ASO (PS), ASYO (PS) and ASO (SPS) show a value of 389 GPa, 396 GPa and 398 GPa respectively in good agreement with literature data on dense polycrystalline alumina (Table 3.1). In the case of the AS (SPS) composites, the Young's modulus remains quite constant with the SiC content in perfect agreement with data calculated using Eq. (3.5) considering a similar modulus (~400 GPa) for silicon carbide. Figure 4.23 presents the measured Young modulus as a function of volume content of silicon carbide of all the homogeneous laminates considered in this work. The trend of AS (PS) and ASY (PS) laminates are decreasing with SiC content, being the Young's moduli lower than the values estimated for fully dense composites. This can be due to the effect of residual porosity which always leads to a decrease in elastic modulus [6]. Considering the Young's moduli obtained for the AS (SPS) laminates as values for fully dense materials and the measured porosity of the pressureless sintered laminates (Table 4.4) quite a good agreement was observed with the trends estimated by the equation Eq. (3.6) proposed by Roberts and Garboczi [100] for overlapping spherical pores (n = 1.65 and $P_0 = 0.818$). Only in the case of the AS10 116

(PS) laminate a deviation was observed probably due to an overestimation of the residual porosity.



Figure 4.23: Young modulus of the homogeneous composites considered in this work as a function of SiC content. Theoretical trends estimated for porous composites by the equation proposed by Roberts and Garboczi are also shown (dashed lines).

The Poisson's ratio calculated for all the homogeneous laminates considered in this work are reported in Table 4.5. The Poisson's ratio of the dense AS (SPS) laminates were calculated by Eq. (3.7). Considering the model of overlapping spherical pores used for the estimation of the elastic modulus of porous materials, the Poisson's ratio of the pressureless sintered laminates where calculated according to Eq. (3.8) with $P_0 = 0.840$ and $v_n = 0.221$.

4.5.5 Hardness and fracture toughness

Vickers hardness and fracture toughness for each homogeneous laminate produced in the present work were measured by indentation technique (Table 4.5). K_{IC} is in fact an important parameter for the estimation of the T-curve and also H is required to compute the ratio E/H in the expression of K_{IC} defined by Eq. (3.10).

Hardness values for the spark plasma sintered composites remain quite equal to the alumina value for any SiC content. On the other hand, pressureless sintered AS laminates exhibit a decreasing trend of hardness with the SiC content (Figure 4.24) which is in a good agreement with the exponential equation:

$$H = H_0 \exp(-5.5P)$$
 Eq. (4.1)

where H is the material hardness, H_o is the value of the dense spark plasma sintered material hardness (Table 4.5) and P is the porosity of the material (Table 4.4). Since an exponential relationship between hardness and porosity has been reported for ceramics [104], the observed hardness are similar to those which can attributed by considering the residual porosity.



Figure 4.24: Hardness of the homogeneous composites considered in this work as a function of SiC content. Theoretical trend estimated for porous composites by an exponential relationship is also shown (dashed line).

Toughness values for the AS0 laminates are equal to about 3 MPa $m^{0.5}$, slightly low compared with previous data on this material [23]. Only limited toughening effect can be observed in the AS (SPS) composites with toughness values as high as 3.5 MPa $m^{0.5}$ for AS25 (SPS). Nevertheless, it is well known that 118

 K_{IC} values obtained by indentation are usually underestimated [101]. Fracture toughness presents a parabolic trend with silicon carbide content in the pressureless sintered laminates (from ~3 MPa m^{0.5} up to ~3.5 MPa m^{0.5} and down to ~3 MPa m^{0.5}) probably related to the deleterious effect of porosity.

4.5.6 Strength

Table 4.6 presents the values of bending strength measured on the homogeneous laminates considered in this work. AS0 (PS), ASY0 (PS) and AS0 (SPS) show a value of 276 MPa, 278 MPa and 311 MPa respectively. The addition of silicon carbide to the spark plasma sintered laminates does not affect the strength of the composites, which exhibit the resistance of pure alumina, around 300 MPa. Figure 4.25 presents the measured flexural strengths as a function of volume content of silicon carbide of all the homogeneous laminates considered in this work. The trend of AS (PS) and ASY (PS) laminates decreases with SiC content since the strength decreases exponentially with an increase in porosity [105]. The strength of porous laminates as a function of porosity is quite in a good agreement with the equation:



Figure 4.25: Bending strength of the homogeneous laminates considered in this work as a function of SiC content. Theoretical trends estimated for porous composites by an exponential equation are also shown (dashed lines).

laminate	$\sigma_b [MPa]$
AS (PS) composites	
0	276 ± 30
5	252 ± 38
10	192 ± 19
15	127 ± 26
20	81 ± 29
ASY (PS) composites	
0	278 ± 25
5	271 ± 47
10	234 ± 32
15	216 ± 59
20	170 ± 31
AS (SPS) composites	
0	311 ± 50
5	267 ± 51
10	269 ± 35
15	296 ± 32
20	300 ± 21
25	280 ± 40
30	312 ± 5

Table 4.6: Bending strength (σ_b) of the homogeneous laminates considered in this

work.

 $\sigma = \sigma_0 \exp(-3P) \qquad \qquad Eq. (4.2)$

where σ_0 is the strength at a zero porosity (AS (SPS)) and P is the material porosity (Table 4.4). Only in the case of the AS10 (PS) laminate a deviation was observed probably due to an overestimation of the residual porosity. 120



(c) AS-I (SPS)





(e) AS-III (SPS)



Figure 4.26: Optical micrographs of the polished sections of the laminates considered in the present work. Laminae composition is shown..

4.6 Engineered laminates

4.6.1 Structure

Figure 4.26 shows the optical micrographs near the surface region of the cross section of representative specimens of all the engineered laminates considered in this work. Perfect layered structures with parallel layers, uniform thickness and good interface union between the constituent tapes have been obtained also when laminae of different composition have been assembled. No defects and no delamination have been shown. Homogeneous composition within the single composite laminae have been observe since SiC grains are clearly visible as white spots and homogeneously distributed in gray alumina layers. These results confirm the goodness and the reliability of the processing procedure used in the present work. Residual porosity and incomplete sintering has been observed in the composite layers of the pressureless sintered laminates (Figure 4.26 and Figure 4.27) due to the detrimental effect of SiC on the alumina sintering, as already discussed in the second chapter.



Figure 4.27: SEM micrograph of the fracture surface of the AS-I (PS) laminate showing the different microstructure of the AS layers with respect to the AS0 layers.

4.6.2 Residual stress profiles

According to the theory presented in the second chapter, Eq. (2.15) and Eq. (2.16) were used to calculate the residual stresses in the five engineered laminates AS-I (PS), ASY-I (PS), AS-I (SPS), AS-II (SPS) and AS-III (SPS). To this purpose, the layer thickness shown in Figure 3.6 and the materials properties of the homogeneous samples presented in Table 4.5 were considered. The results of such calculations are presented in Table 4.7. In this table the same layer sequence shown in Figure 3.6 was considered, in order to use a representation more similar to the actual laminate structure. For this reason some results seem to be duplicated, the same stress values being obviously obtained for the same layer material.

The engineered laminate AS-I (PS) presents a thin surface layer and the core material (AS0) in slight tension (16 MPa) while the most compressed layer is AS20 which shows a compression of 105 MPa. A thin intermediate compressive layer (AS10) is placed before and beyond AS20. Similar stresses were obtained in the ASY-I (PS) laminate, the highest compressive amplitude (-167 MPa) being reached in the ASY20 layer.

Higher residual stress level is produced in the spark plasma sintered laminates where the composing layers are dense AS composites. The most compressed layer in the AS-I (SPS) and AS-III (SPS) laminates is AS20 which presents a residual compression of -402 MPa and -390 MPa respectively, while a limited tensile layer (AS0 exhibiting 23 MPa and 37 MPa respectively) is placed on the external surface. In a similar way, the most compressed layer in the AS-II (SPS) laminate is AS30 which presents a residual compression of -502 MPa while the external tensile layer AS0 exhibit a residual stress of 28 MPa.

A phenomenon sometimes observed in high-compressed layers is the wellknown edge-cracking (Figure 2.19(c)). As explained in the second chapter, a highly localized tensile stress perpendicular to the layer plane must be present in the residual biaxial-compressed layers to satisfy the stress-free boundary condition of the external surfaces at the laminate edge. Such stress is localised near the free surface and is able to propagate defects only for a limited depth within the laminate in absence of further applied stresses.

Table 4.7: Residual stresses calculated for the engineered laminates considered inthis work. The calculated critical thickness (t_c) for edge cracking of the mostcompressed layer is also shown.

_	A	S-I (PS)			AS	Y-I (PS)	
i	layer	h	σ	i	layer	h	σ
		[µm]	[MPa]			[µm]	[MPa]
1	AS0	40	16	1	AS0	40	26
2	AS10	40	-94	2	ASY10	40	-153
3	AS20	40	-105	3	ASY20	40	-167
4	AS10	40	-94	4	ASY10	40	-153
5	AS0	680	16	5	AS0	680	26
$t_c =$	1837 µm			$t_c =$	780 µm		
	A.	S-I (SPS)			AS	-II (SPS)	
i	layer	h	σ	i	layer	h	σ
		[µm]	[MPa]			[µm]	[MPa]
1	AS0	30	23	1	AS0	30	28
2	AS10	25	-186	2	AS20	20	-398
3	AS20	30	-402	3	AS30	20	-502
4	AS10	25	-186	4	AS20	20	-398
5	AS0	890	23	5	AS0	895	28
$t_c =$	163 µm			$t_c = 1$	105 µm		
	AS	-III (SPS)					
i	layer	h	σ				
		[µm]	[MPa]				
1	AS0	30	37				
2	AS10	25	-173				
3	AS20	30	-390				
4	AS10	25	-173				
5	AS0	525	37				

 $t_c = 173 \ \mu m$



Figure 4.28: Residual stress profile calculated for the AS-I (PS) laminate.



Figure 4.29: Residual stress profile calculated for the ASY-I (PS) laminate.



Figure 4.30: Residual stress profile calculated for the AS-I (SPS) laminate.



Figure 4.31: Residual stress profile calculated for the AS-II (SPS) laminate.



Figure 4.32: Residual stress profile calculated for the AS-III (SPS) laminate.

According to the multilayered structure of each engineered laminates and to the residual stress intensities, the critical layer thickness t_c below which edge cracking does not occur, was calculated by Eq. (2.21) for the most compressed layers to investigate the occurrence of such phenomenon. Edge cracking was not expected for each engineered laminate studied in this work.

By considering the actual stacking order of the layers, the residual stresses can be also plotted in a graph to point out the actual dependence of the stress on depth and to show the trend of the step-wise residual stress profile more clearly. The five stress profiles corresponding to the engineered laminates are shown in Figure 4.28, Figure 4.29, Figure 4.30, Figure 4.31 and Figure 4.32. A square root abscissa was considered to make the comparison with the diagrams showing the apparent fracture toughness easier.

4.6.3 Apparent fracture toughness and expected mechanical behaviour

The knowledge of the residual stress profile for each laminate allowed to estimate the T-curve, the trend of the apparent fracture toughness as a function of crack length. It is useful to remind here that for surface cracks depth x and crack length c represent the same spatial dimension. As described in second chapter, the calculation of the apparent fracture toughness was performed solving Eq. (2.17) and Eq. (2.18). For each laminate, the design strength and threshold stress were calculated by Eq. (2.19) and Eq. (2.20), respectively.

Figure 4.33 shows the T-curve estimated for the AS-I (PS) laminate as a function of crack length. After a decreasing portion of the curve corresponding to the surface layer extent, the T-curve raises in the first compressive intermediate AS10 layer. Then, a discontinuity in the T-curve consisting in a decrease of the apparent fracture toughness from 4.5 MPa $m^{0.5}$ to 3.9 MPa $m^{0.5}$ in the external surface of the most compressed layer AS20 is present due to the significant reduction in intensity of the fracture toughness from the AS10 (3.5 MPa m^{0.5}) to the AS20 (2.9 MPa $m^{0.5}$) layer. Then, the T-curve increases up to the internal surface of the inner AS10 layer with another sharp discontinuity at the interface between the AS20 lamina and the internal AS10 layer and decreases again for deeper position. Since the conditions of stable propagation of crack are satisfied when the increase of toughness with crack extension is larger than the corresponding increase of stress intensity factor (Eq. (2.7)), the maximum depth at which surface flaws grow in a stable manner at the maximum stress which can be applied to the laminate AS-I (PS) before failure corresponds to a point within the first compressed layer AS10. The following lower monotonic increase of the apparent fracture toughness could allow stable growth of deeper cracks, but at stresses between the threshold stress and the maximum stress. The applied stress intensity factor corresponding to the maximum stress and to the threshold stress in bending are shown as lines in Figure 4.34. As calculated, the apparent fracture toughness of the multilayer reaches 5.5 MPa m^{0.5}, but only the T-curve portion with up to 4 MPa m^{0.5} acts for the stable propagation of surface cracks in the range between 40 μ m and 53 μ m at the maximum stress of 276 MPa (Table 4.8). Table 4.8 shows also the threshold stress expected by this laminate, equal to 214 MPa.

From Figure 4.34 similar considerations can be made regarding the T-curve behaviour of the ASY-I (PS) laminate. The curve decreases in correspondence to the surface tensile layer, then raises in the compressive layers with a discontinuity in the most compressed layer ASY20 due to the mismatch in the fracture toughness of the ASY10 (3.5 MPa m^{0.5}) and ASY20 (3.0 MPa m^{0.5}) layers. Then, the curve decreases

again for deeper position. In this case, only the T-curve portion with up to 5.1 MPa $m^{0.5}$ acts for the stable propagation of surface cracks in the range between 40 μ m and 80 μ m at the maximum stress of 290 MPa (Table 4.8). The threshold stress expected by this laminate is equal to 204 MPa (Table 4.8).

Figure 4.35 shows the T-curve estimated for the AS-I (SPS) laminate. In this case, after a decreasing portion of the curve corresponding to the surface tensile layer, the T-curve raises in a quite a monotonic way up to 8 MPa m^{0.5} at the internal surface of the most compressed layer (AS20) and decreases again for deeper position. Such point corresponds therefore to the maximum depth which defects growing in a stable manner can reach and also to the condition of the maximum stress which can be applied to the laminate before failure. The calculated values for the design strength and the threshold stress in bending as well as the stable crack growth interval for AS-I (SPS) are 437 MPa, 252 MPa and 30–85 μ m, respectively, as shown in Table 4.8.

From Figure 4.36 similar considerations can be made regarding the T-curve behaviour of the AS-II (SPS) laminate. The qualitative trend is similar to the previous example except for an additional slight toughness increase in the internal intermediate layer AS20. However, the applied stress intensity factor corresponding to the internal surface of the most compressed layer (AS30) raises in a steeper way than the T-curve in such intermediate lamina. Hence, also in this case the maximum depth at which defects grow in a stable manner corresponds to the internal depth of the most compressed layer. The apparent fracture toughness of the multilayer reaches a value as high as 8.8 MPa m^{0.5} at 70 µm (Table 4.8). Table 4.8 shows also the maximum and threshold stresses expected by this laminate, equal to 528 MPa and 248 MPa, respectively. A stable propagation of surface cracks in the range between 30 µm and 70 µm are therefore expected for this laminate.

Figure 4.37 presents the T-curve estimated for the AS-III (SPS) laminate. After an initial decrease due to the AS0 tensile surface layer the apparent fracture toughness starts to increases with depth up to a maximum value of 7.8 MPa m^{0.5} achieved at 85 μ m (Table 4.8). The maximum and threshold stresses expected for this laminate, are 425 MPa and 239 MPa, respectively (Table 4.8).

Table 4.8: Threshold stress (σ_{th}), design strength (σ_d), shortest defect size which could undergo to stable propagation at stresses lower than the design strength (c_0), stable crack growth interval ([$c_{th} - c_d$]) and estimated crack sizes interval ([$c_{min} - c_d$])

	σ_{th}	σ_d	c_0	$[c_{th} - c_d]$	$[c_{min} - c_{max}]$
	214	276	25	[µm]	20, 52
AS-I (PS)	214	276	25	40-53	20-52
ASY-I (PS)	204	290	21	40-80	20-52
AS-I (SPS)	252	437	11	30-85	15–54
AS-II (SPS)	248	528	7.4	30-70	15–54
AS-III (SPS)	239	425	11	30-85	16-66

 $c_{max}]).$



Figure 4.33: T-curve estimated for the AS-I (PS) laminate. Lines corresponding to the threshold and failure conditions are also shown. The bar indicates the actual range of starting crack sizes.



Figure 4.34: T-curve estimated for the ASY-I (PS) laminate. Lines corresponding to the threshold and failure conditions are also shown. The bar indicates the actual range of starting crack sizes.



Figure 4.35: T-curve estimated for the AS-I (SPS) laminate. Lines corresponding to the threshold and failure conditions are also shown. The bar indicates the actual range of starting crack sizes.



Figure 4.36: T-curve estimated for the AS-II (SPS) laminate. Lines corresponding to the threshold and failure conditions are also shown. The bar indicates the actual range of starting crack sizes.



Figure 4.37: T-curve estimated for the AS-III (PS) laminate. Lines corresponding to the threshold and failure conditions are also shown. The bar indicates the actual range of starting crack sizes.

4.6.4 Weibull analysis

The mechanical behaviour of the five engineered laminates is presented here. Each laminate is compared by using the Weibull analysis to the corresponding homogeneous monolithic alumina laminate to highlight any improvement in the mechanical performances due to its special architecture.

The average bending strength measured on the AS-I (PS) samples is equal to 324 ± 30 MPa (Table 4.9), the coefficient of variation (COV) being 9%. For comparison, the corresponding homogeneous AS0 (PS) laminate presents a COV equal to 11%. The decrease of strength scatter is also evident if one compares the Weibull plots for the laminates AS-I (PS) and AS0 (PS) shown in Figure 4.38. The Weibull modulus, m, is the fundamental statistical parameter used in the field of structural design for brittle materials, the lower the modulus the wider the scatter of strength data and the lower the mechanical reliability. The engineered AS-I (PS) laminate presents a Weibull modulus equal to 13 while a value of 11 was measured for the AS0 (PS) (Table 4.9). The minimum and the maximum strength value in the distribution are also shown in Table 4.9. The spreading of strength data decreases from 126 MPa for the AS0 (PS) to 103 MPa for the AS-I (PS) and this corresponds to a relative strength variability ($\Delta\sigma/\sigma$) decreasing from 0.38 down to 0.27. The most interesting point regards the low strength tail of the distribution in the case of the AS-I (PS) laminate, which is much steeper than the remaining part of the data, giving rise to a knee in the curve. The actual trend of the AS-I (PS) data resembles indeed the typical Weibull plot obtained after proof testing [6,8] (Figure 2.3). To account for the presence of such knee and to explain the residual strength scatter, it is possible to observe that the shortest crack length, which can grow in a stable fashion, as discussed in the second chapter, is not zero, the actual value being a function of the apparent fracture toughness curve. If the kinetics phenomena are neglected, such crack size can be obtained from the intersection of the applied stress intensity factor curve corresponding to the maximum stress at instability with the Tcurve. In this manner a minimum value of 25 µm can be estimated for the AS-I (PS) laminate (Figure 4.33 and Table 4.8). The actual range of crack lengths in the surface layer was estimated using Eq. (2.1) and considering the minimum and

maximum strength measured on the homogeneous AS0 (PS) laminates (Table 4.9). An interval of crack sizes between 20 μ m and 52 μ m was calculated using a fracture toughness value of 2.9 MPa m^{0.5} for alumina (Table 4.5). Some of the defects are therefore shorter than 25 μ m and propagate at higher stresses than the maximum applied stress estimated by design, producing a scatter similar to homogeneous ceramic material. The designed stress, 276 MPa (Table 4.8), corresponds therefore to the minimum value for the strength data, being indeed in a very good agreement with the minimum strength measured by the experiments (Table 4.9).



Figure 4.38: Weibull plot for bending strength data measured on the pressureless sintered engineered laminates AS-I (PS), ASY-I (PS) and on the corresponding alumina laminate. The calculated Weibull modulus is also shown.

The ASY-I (PS) laminate possesses an average bending strength, a coefficient of variation (COV) and a Weibull modulus equal to 309 ± 25 MPa, 8 and 15, respectively (Table 4.9). The corresponding homogeneous AS0 (PS) laminate presents a COV equal to 11% and a Weibull modulus equal to 11 (Table 4.9). Also in this case, the decrease of strength scatter is highlighted by the Weibull plots for the laminates ASY-I (PS) and AS0 (PS) shown in Figure 4.38. The T-curve trend of the ASY-I laminate is similar to the one exhibited by the AS-I (PS) laminate with a low strength tail much steeper than the remaining part of the data. This behaviour is

related again to the shortest crack length, which can grow in a stable fashion, estimated as equal to 21 μ m (Figure 4.34 and Table 4.8). The actual range of crack lengths in the surface layer was estimated as equal to 20–52 μ m. Hence, some of the defects could be shorter than 21 μ m and propagate at slight higher stresses than the maximum applied stress estimated by design as equal to 290 MPa (Table 4.8). Therefore, a certain scatter of strength data of this laminate is expected while the minimum strength (271 MPa) measured by the experiments (Table 4.9) is quite in good agreement with the designed stress.

The laminate AS-I (SPS) shows an average bending strength equal to $328 \pm$ 49 MPa (Table 4.9), a minimum and maximum stress equal to 251 MPa and 432 MPa, respectively, and a Weibull modulus equal to 8. The laminate AS-II (SPS) exhibits an average bending strength equal to 373 ± 82 MPa (Table 4.9), a minimum and maximum stress equal to 286 MPa and 506 MPa, respectively, and a Weibull modulus equal to 5. For comparison, the corresponding homogeneous alumina laminate AS0 (SPS) has an average bending strength equal to 311 ± 50 MPa (Table 4.9), a minimum and maximum stress equal to 205 MPa and 386 MPa, respectively, and a Weibull modulus equal to 7. Despite the lack of reliability increase of the engineered laminates with respect to alumina, an appreciable shift of the strength data toward higher values is observed for AS-I (SPS) and AS-II (SPS) multilavers (Table 4.9 and Figure 4.39). If one compares the average strength of the AS-I (SPS) and AS-II (SPS) laminates, 328 MPa and 373 respectively, with the bending strength (437 MPa and 528 MPa) predicted for these profiles (Table 4.8), it is possible to observe that there is not a good agreement. The measured minimum and maximum stresses of the laminate AS-I (SPS) are equal to 251 MPa and 432 MPa respectively, and are included in the range 252–437 MPa arranged by the threshold stress and the design stress (Table 4.8 and Table 4.9). Analogously, the measured minimum and maximum stresses of the laminate AS-II (SPS) are equal to 286 MPa and 506 MPa respectively, and are included in the range 248-528 MPa arranged by the threshold stress and the design stress of this laminate (Table 4.8 and Table 4.9). No strength data exceeding the maximum design stress was measured for both laminates. In addition, the Weibull plot of the AS-I (SPS) laminate exhibited a low strength tail much steeper than the remaining part of the data at about 251 MPa, pointing out the presence of a threshold stress which is in agreement with the calculated value of 252 MPa. In a similar way, the AS-II (SPS) laminate showed a low strength tail at about 286 MPa which is in agreement with the calculated value of 248 MPa. All these results can be explained by the presence of inherent defects of dimensions shorter than the stability interval, included between c_0 (11 µm and 7.4 µm, for AS-I (PS) and AS-II (PS) respectively) and cth (30 µm) that propagate in unstable fashion for stresses between σ_{th} (252 MPa and 248 MPa, respectively) and σ_d (437 MPa and 528, respectively) due to their acceleration. Indeed, if the kinetics phenomena are not neglected such cracks can growth up to a length greater than c_d (85 μm and 70 µm, respectively) leading to fracture for stresses lower than the design stress. The Tcurve can not be effective, in fact, to stop the growing cracks if they possess a finite crack speed and they can overcome such barrier at lower stress levels than what theoretically estimated. Since the minimum defect equal to 15 μ m is longer than c₀ (11 μ m and 7.4 μ m, respectively) no strength data higher than the design stress are observed. Hence, the mechanical behaviour of these two laminates is in good agreement with the calculated T-curves and estimated inherent crack sizes, if kinetics phenomena are considered.



Figure 4.39 Weibull plot for bending strength data measured on the thick spark plasma sintered engineered laminates AS-I (SPS), AS-II (SPS) and on the corresponding alumina laminate. The calculated Weibull modulus is also shown.

Analogous behaviour is expected for the thin spark plasma sintered laminate AS-III (SPS) since the estimated flaws dimensions are partially situated in the stable growth range and partially in the range for unstable propagation at stresses between the threshold stress and the design stress, if kinetics phenomena are considered (Figure 4.37). In fact, the minimum defect, which can propagate in a stable fashion and the natural crack sizes were calculated in this case as 11 µm and 16-66 µm, respectively (Table 4.8). The average bending strength measured on the AS-III (SPS) samples is equal to 327 ± 30 MPa (Table 4.9). This corresponds to a coefficient of variation of 9%. For comparison, the bending strength of the homogeneous AS0^{III} (SPS) laminates is equal to 290 ± 46 MPa (COV = 16%). The range of strength data is shown in Table 4.9. If one compares AS0^{III} (SPS) with AS-III (SPS) the scatter of strength data decreases from less than 200 MPa to about 100 MPa and the relative strength variability from 0.50 down to 0.28. Weibull plots for the AS-III (SPS) and ASO^{III} (SPS) laminates are shown in Figure 4.40 and the Weibull modulus is presented in Table 4.9 being equal to 8 for the AS0^{III} (SPS) laminate and 13 for the AS-III (SPS) laminate.



Figure 4.40: Weibull plot for bending strength data measured on the thin spark plasma sintered engineered laminates AS-III (SPS) and on the corresponding alumina laminate. The calculated Weibull modulus is also shown.

Such difference represents an improvement in the mechanical reliability of the material. Therefore, despite the presence of defects smaller than the stability range, most defects are supposed to undergo to stable growth before the laminate failure and increased reliability can be observed. Indeed, the mechanical strength trend of this laminate is again well explained by the design.

The differences between the actual and calculated strength values can be related to errors in the evaluation of layer thickness or lamina properties, particularly for the thermal expansion coefficient. This parameter is the actual driving force for the development of a residual stress profile and it exerts a direct influence on the amplitude of the layer residual stresses. The layer thickness also influences the bending strength, its effect being twofold: both single residual stress amplitude and depth of internal layers are function of the actual thickness of the sintered laminas, the apparent fracture toughness changing accordingly.

Table 4.9: Number of strength data (N), average strength (σ_b), coefficient of variation (COV), minimum (σ_{min}) and maximum (σ_{max}) stress, relative strength variability ($\Delta\sigma/\sigma$) and Weibull modulus (m) observed for the engineered laminates and the corresponding alumina laminates considered in this work.

	Ν	$\sigma_b [MPa]$	COV [%]	σ _{min} [MPa]	σ_{max} [MPa]	Δσ/σ	т
Pressureless sint	ered l	aminates					
ASO (PS)	30	$276\ \pm 30$	11	203	329	0.38	11
AS-I (PS)	27	$324\ \pm 30$	9	272	375	0.27	13
ASY-I (PS)	27	$309\ \pm 25$	8	271	364	0.25	15
Thick spark plass	ma sir	ntered laminate	S				
ASO (SPS)	20	$311\ \pm 50$	16	205	386	0.47	7
AS-I (SPS)	17	$328\ \pm 49$	15	251	432	0.42	8
AS-II (SPS)	12	$373\ \pm 82$	22	286	506	0.43	5
Thin spark plasma sintered laminates							
ASO ^{III} (SPS)	26	$290\ \pm 46$	16	186	373	0.50	8
AS-III (SPS)	26	$327\ \pm 30$	9	271	375	0.28	13

4.6.5 *Post-indentation strength*

To investigate the effect of longer cracks and damage resistance on the mechanical behaviour of laminates, Vickers indentations were produced at different loads as described in the third chapter. Special attention was paid on the influence of indentation load on strength and a discussion about the damage tolerance shown by the engineered multilayers with respect to the homogeneous laminates was presented.



Figure 4.41: Post-indentation strength data as a function of indentation load for the pressureless sintered engineered laminates considered in this work and the corresponding alumina laminates.

Figure 4.41 shows the average bending strength measured on indented samples for the AS-I (PS), ASY-I (PS) and AS0 (PS) laminates. As summarised in Table 4.10, the strength of indented AS-I and ASY-I samples remains constant for different indentation loads, being equal to about 276 MPa and 322 MPa, respectively, whereas decreases in the case of the homogeneous AS0 (PS) down to 134 MPa for indentations at 100 N. The unvaried strength trend observed for the engineered laminates represents the ideal damage tolerant material, since the mechanical behaviour is not influenced at all by indentation, at least in the range of defects produced by indentation up to 100 N. The average bending strength on

indented samples is in optimum agreement with both the design value, 276 MPa and 290 MPa respectively (Table 4.8). In addition, these results can be considered as an evidence of the presence of stable growth phenomena occurring in the same crack interval due to the presence of a T-curve behaviour. To investigate further this topic, 1 sample of AS-I (PS) and ASY-I (PS) were broken after being indented at 150 N. Lower bending strength, as equal to 174 MPa and 192 MPa, respectively, were observed (Table 4.10). In this case, the cracks produced by indentation have probably overcome the maximum depth of the stable growth range, vanishing the reinforcing effect of the compressive residual stress profile.



Figure 4.42: Post-indentation strength data as a function of indentation load for the thick spark plasma sintered engineered laminates and the corresponding alumina laminates.

The bending strength obtained from indented samples of the AS-I (SPS), AS-II (SPS) and AS0 (SPS) laminates is shown in Figure 4.42 and the numerical results are presented in Table 4.10. Also in these last cases the mechanical resistance of the engineered laminates, ~310 MPa and ~510 MPa, respectively, does not depend on indentation load in the considered load range and this corresponds to an ideal damage-tolerant material. The average bending strength on indented samples of the AS-I (SPS) laminate is slightly lower than the design values, 437 MPa, (Table

4.8) but in really good agreement with the strengths measured on non-indented samples, 328 MPa (Table 4.9). On the other hand, the average bending strength on indented samples of the AS-II (SPS) laminate is really in good agreement with the design values, 528 MPa (Table 4.8), being dramatically higher than the strengths measured on non-indented samples, 373 MPa (Table 4.9), pointing out that deeper cracks, introduced in the materials by indentations, can undergo to stable propagation as predicted by design.

The strength of indented samples of the AS-III (SPS) and AS0^{III} (SPS) laminates as a function of the indentation load is presented in Figure 4.43. Also in this case, the bending strength of the engineered multilayered laminate, ~350 MPa, is not depending on indentation load, whereas the strength of the homogeneous AS0 (SPS) laminate decreases with load down to 178 MPa for indentation at 100 N (Table 4.10). In addition, the average bending strength on indented samples is slightly lower than the design value, 425 MPa, (Table 4.8) and in good agreement with the strength measured on non-indented samples, 327 MPa, (Table 4.9).



Figure 4.43: Post-indentation strength data as a function of indentation load for the thin spark plasma sintered engineered laminates considered in this work and the corresponding alumina laminates.

The zero-slope behaviour is therefore shown by all the laminates, being more evident for the AS-II (SPS) multilayer, and the damage tolerance is confirmed in the considered load range. Differences between the calculated strengths and the strengths measured on indented samples can be related again to errors in the evaluation of layer thickness or lamina properties that change the apparent fracture toughness curve respect to the one calculated. In addition, some cracks grew from inherent flaws and not from indentation sites, hindering the measure of the maximum design stress. Despite these observable differences between the post indentation strengths and the design stresses, the mechanical behaviour of the engineered laminates is well explained by the design used in this work and the related considerations.

Table 4.10: Post-indentation strength of the engineered multilayers and of the corresponding alumina homogeneous laminates considered in this work.

Indentation loads	0 N	10 N	30 N	100 N	150 N		
Pressureless sintered	laminates						
ASO (PS)	$276\ \pm 30$	186 ± 32	148 ± 16	134 ± 18	-		
AS-I (PS)	$324\ \pm 30$	$276\ \pm 52$	288 ± 47	264 ± 26	174		
ASY-I (PS)	$309\ \pm 25$	$305\ \pm 38$	$336\ \pm 39$	$325\ \pm 44$	192		
Thick spark plasma s	intered lamind	ates					
ASO (SPS)	$311\ \pm 50$	$278\ \pm 20$	$228\ \pm 31$	$177\ \pm 23$	-		
AS-I (SPS)	$328\ \pm 49$	$302\ \pm 20$	$317\ \pm 66$	316 ±36	-		
AS-II (SPS)	$373\ \pm 82$	-	523	501	-		
Thin spark plasma sintered laminates							
AS0 ^{III} (SPS)	$290\ \pm 46$	$284\ \pm 35$	$248\ \pm 49$	$178\ \pm 14$	-		
AS-III (SPS)	$327\ \pm 30$	$352\ \pm 32$	355 ± 5	$340\ \pm 20$	-		
4.6.6 Stable growth: expectations and experimental evidences

In addition to the improvement of the damage resistance, the presence of stable growth phenomena is also expected for materials presenting a T-curve behaviour. In order to look for confirmations of the existence of a range of stable crack growth in the optimised laminates, a fractographic analysis was performed on some broken samples of all the laminates considered in this work.

In the homogeneous samples the typical fracture mirror was always present, its size increasing when strength decreases as expected by the larger size of the critical flaw (Figure 4.44). Conversely, the engineered multilayered laminates showed different and specific features on the fracture surface either in the case of indented and non-indented samples. Figure 4.45 and Figure 4.46 present the fracture surfaces observed in the case of the engineered laminates. A special feature can be observed in all the pictures: a smooth flat narrow region extending from edge-to-edge (through-thickness geometry) is present just beneath the tensile surface (top), while the reinitiating crack fracture mirror starts below this rectangular area. In particular, the AS-I (SPS) and AS-II (SPS) laminates exhibit this feature, evidence of surface cracks stable growth, only at higher loads, starting from about 300 MPa and 490 MPa, respectively. In the case of the AS-III laminate, stable growth has been observed to occur at all the observed strength.

Figure 4.47 shows a SEM image of a section of the fracture surface of a AS-III (SPS) sample where the smooth region under the tensile surface is clearly evident. The maximum depth of stable growth of defects pointed out by the dashed line is in good agreement with the design value (85 μ m). The lack of a fracture mirror starting from the external surface, combined with the presence of a through-thickness arrest mark in correspondence of a sharp change of surface roughness suggest that stable growth phenomena actually occur in the engineered laminates.

In addition, the inner depth of the flat region described above is quite similar to the point which defines the maximum depth of stable growth expected by design. What actually seems to happen is that the critical crack follows a two stage propagation: a first stage with a moderately low speed occurs up to a certain depth.



(b) AS0 (SPS)





Figure 4.44: Fracture surfaces of homogeneous alumina samples. Typical fracture surface of ceramic materials with fracture mirror (indicated by arrow) in correspondence of the tensile surface (T) is observable.

(a) AS-I (PS) (b) ASY-I (PS) T T 2 mm

(c) AS-I (SPS)

(d) AS-II (SPS)



(e) AS-III (SPS)



Figure 4.45: Fracture surfaces of engineered laminates samples. A smooth narrow region with a through thickness geometry is present just beneath the tensile surface (indicated by T). Reinitiating crack fracture mirror is indicated by arrow.



(c) AS-I (SPS)

(d) AS-II (SPS)



(e) AS-III (SPS)



Figure 4.46: Particular of fracture surfaces of engineered laminates samples. A smooth narrow region with a through thickness geometry is present just beneath the tensile surface (indicated by T).

On a second time, when critical condition for unstable propagation is reached, crack restarts leaving a fracture surface similar to what observed in the case of homogeneous samples broken at high loads which is shifted toward the inner part of the laminate.

In conclusion, in addition to a high damage resistance and a reduced strength scatters stable growth phenomena for surface cracks seem to occur in the depth range corresponding to what expected by the trend of the apparent fracture toughness estimated by design. This was verified either for natural flaws and indentation cracks and a T-curve behaviour for the optimised multilayered laminates can be advanced accordingly.



Figure 4.47: SEM micrograph showing a particular of the fracture surface of a AS-III (SPS) sample. The maximum depth of stable crack propagation is highlighted by the dashed line. The surface in tension is marked with T.

Conclusion and future perspectives

In the present work two routes to prepare layered structures with strong interfaces in the system Al_2O_3/SiC have been shown. A processing method, which utilizes conventional techniques like tape casting, lamination and pressureless sintering has been developed for fabricating Al_2O_3/SiC laminates with SiC content up to 20 vol%, also by using yttria as sintering aid. The weight loss generally observed in pressureless sintering these composites was minimized by optimizing the sintering conditions and by using a 50 mol% Al_2O_3/SiC powder bed. In addition, Spark Plasma Sintering of tape casted composite laminae has been used as innovative sintering technology to produce fully dense and thin Al_2O_3/SiC laminates with SiC load up to 30 vol%.

By modifying the composition and the architecture of Al₂O₃/SiC composite laminae, five engineered multilayers characterized by tailored residual stress profiles have been produced by pressureless sintering or Spark Plasma Sintering. The engineered laminates have been designed and fabricated to support bending loads and to promote the propagation of surface defects in a stable manner thanks to a Tcurve behaviour. The results of the mechanical characterization of the engineered laminates compared to the behaviour of simple homogeneous materials, proved that the arising of residual stresses influences the multilayers fracture resistance. Indeed, the engineered laminates are stronger than parent monolithic alumina and are characterized by a minimum mechanical resistance and surface damage insensitivity, also when macroscopic cracks are introduced by Vickers indentations at loads as high as 100 N. Some laminates exhibit reduced scatter and higher Weibull modulus, which implies superior reliability.

Examination of fractographic features in the engineered laminates showed a constant depth smooth area just beneath the tensile surface which can be attributed to the stable growth of surface cracks within the surface layers in residual compressive stress. Such peculiar crack propagation, correlated to the laminate architecture, could be associated to the mechanical performances of the engineered laminates and is responsible for the observed damage tolerance.

The results of this study are likely to find practical applications in the field of mechanical behaviour of advanced ceramic composites. Among the future perspectives originated by this work, one point concerns with the tailoring of proper laminates architectures able to force most of inherent surface flaws to stable growth. A future challenge could be the study of rupture behaviour of these materials at high temperatures. The production of components of complex shape as shells or tubes, with such microstructural architecture could be also investigated.

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Appendix: Code of the numerical algorithm

The code of the numerical algorithm implemented in Mathematica® and used in this work is listed in the present Appendix. The code regards the estimation of the T-curve produced by a given step-wise residual stress profile for a sharp edge crack under bending loading and the calculation of the maximum and threshold stress for stable crack propagation. To make the identification of variables and flags meaning easier, the instructions list is reported here with the input numerical values used in this work for the AS-III (SPS) T-curve. Fracture toughness, stress and length dimensions are reported in MPa m^{0.5}, MPa and µm, respectively.

T-CURVE BY STEP-WISE RESIDUAL STRESS PROFILE

LAMINATE IMPUT DATA layer=5 KIC={3.0,3.3,3.3,3.3,3.0} EMod={398,394,366,394,398} NuMod={0.23,0.224,0.217,0.224,0.23} alpha={8.8,8.45,8.03,8.45,8.8} laythick={30,25,30,25,525} DeltaT=-1175 YFac=1.12147 depth={0,0,0,0,0} lasttens=1 mostcomp=3 delta={0,0,0,0,0}

STRESS PROFILE CALCULATION EModStar=EMod/(1-NuMod) i=1;While[i<layer+1,

 $depth=ReplacePart[depth,Sum[Extract[laythick,k],{k,1,i}],i];i++]$

depth

EModStar*laythick*alpha

EModStar*laythick

i=1;While[i<layer+1,

```
alphaAvNom = Sum[Extract[EModStar*laythick*alpha,k], \{k,1,i\}]; i++]
```

```
i=1; While [i < layer+1, alpha AvDen = Sum [Extract [EModStar*laythick, k], \{k, 1, i\}]; i++]
```

```
alphaAv=alphaAvNom/alphaAvDen
```

```
stress=EModStar*1000*(alphaAv-alpha)*10^-6*DeltaT
```

```
depth=Prepend[depth,0]
```

stress=Prepend[stress,0]

d2=depth^0.5

T-CURVE CALCULATION

i=1;While[

```
i<layer+1,{delta=
```

```
ReplacePart[delta, Extract[stress, i+1]-Extract[stress, i], i] \}; i++]
```

delta

```
M=IdentityMatrix[layer]
```

```
i=1;While[
```

```
i<layer+1,{M=
```

ReplacePart[M,

```
2*YFac*(x/Pi)^0.5/1000*
```

```
Extract[delta,i]*(Pi/2-ArcSin[Extract[depth,i]/x]),i];
```

```
Print[Extract[M,i]]};i++]
```

M2=M

```
i=1;While[i<layer+1,M2=ReplacePart[M2,Sum[Extract[M,k],{k,1,i}],i];i++]
```

x=g^2

M2

```
apparentK=Table[{0,0}, {j,0,Extract[d2,layer+1]*10}]
```

i=1

k=1

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```
w=0.1;While[
```

```
w<Extract[d2,layer+1],{If[w>Extract[d2,i+1],i=i+1];g=w;
apparentK=ReplacePart[apparentK,{w,Extract[KIC,i]-N[Extract[M2,i]]},k];
Print[Extract[apparentK,k]];k=k+1};w=w+0.1]
Clear[g]
```

MAXIMUM STRESS CALCULATION

```
g=Extract[d2,mostcomp+1]

Kmax=Max[{Extract[KIC,mostcomp]-Extract[M2,mostcomp],

Extract[KIC,mostcomp+1]-Extract[M2,mostcomp+1]}]

stressmaxapprox=Kmax/(YFac*Pi^0.5*g)*1000

stressmaxtrue=FindRoot[YFac*Pi^0.5*s/1000*g-

Kmax\[Equal]0,{s,stressmaxapprox}]
```

THRESHOLD STRESS CALCULATION

```
g=Extract[d2,lasttens+1]

Kmin=Min[{Extract[KIC,lasttens]-Extract[M2,lasttens],

Extract[KIC,lasttens+1]-Extract[M2,lasttens+1]}]

stressminapprox=Kmin/(YFac*Pi^0.5*g)*1000

stressmintrue=FindRoot[YFac*Pi^0.5*s/1000*g-

Kmin\[Equal]0,{s,stressminapprox}]

Clear[g]
```

```
PRINT CORRESPONDING APPLIED STRESS INTENSITY FACTORS
appliedKmax=N[YFac*Pi^0.5*s/1000*g/.stressmaxtrue]
Clear[s]
appliedKmin=N[YFac*Pi^0.5*s/1000*g/.stressmintrue]
```

PRINT MAXIMUM AND THRESHOLD STRESS VALUES stressmaxtrue stressmintrue

GRAPHICS

<<"Graphics`FilledPlot`"

```
p=IdentityMatrix[layer]
```

```
i=1;While[i<layer+1,
```

p=ReplacePart[p,

FilledPlot[

Evaluate[Extract[KIC,i]-Extract[M2,i]],{g,Extract[d2,i],

 $Extract[d2,i+1]\}, PlotRange->\{0,25\}, Fills \ [Rule] \{GrayLevel[.8]\},$

Curves\[Rule]Front,DisplayFunction->Identity,

 $PlotStyle \[Rule]Hue[0.6]], i]; i++]$

p=Append[p,

Plot[appliedKmax, {g,0,Max[d2]}, DisplayFunction \[Rule]Identity,

PlotStyle\[Rule]Hue[1.0]]]

p=Append[p,

Plot[appliedKmin,{g,0,Max[d2]},DisplayFunction\[Rule]Identity,

```
PlotStyle\[Rule]Hue[1.0]]]
```

 $Show[p,DisplayFunction\[Rule]\] SDisplayFunction, GridLines\[Rule]\] Automatic,$

```
Background\[Rule]GrayLevel[0.85]]
```

```
p2=IdentityMatrix[layer]
```

```
i=1;While[i<layer+1,
```

p2=ReplacePart[p2,

FilledPlot[

Evaluate[Extract[stress,i+1]],{g,Extract[d2,i],Extract[d2,i+1]},

PlotRange\[Rule]{Min[stress]*1.5,-Min[stress]*1.5},

DisplayFunction\[Rule]Identity,

PlotStyle\[Rule]{Hue[0.6],Dashing[{0.01,0.01}]]},i];i++]

Show[p2,DisplayFunction\[Rule]\$DisplayFunction,GridLines\[Rule]Automatic,

 $Background \ [Rule] Gray Level [0.85], Axes Origin \ [Rule] \{0, Min[stress]^{1.5}\}]$

Clear[g,x,i]

Scientific Production

F. De Genua, V. M. Sglavo, "High strength engineered alumina-silicon carbide laminated composites by Spark Plasma Sintering" in Procedia Engineering, 10 2621-2626 (2011).

V. M. Sglavo, F. De Genua, A. Conci, R. Ceccato, R. Cavallini, "Influence of curing temperature on the evolution of magnesium oxychloride cement" in Journal of Material Science, 46 [20] 6726-6733 (2011).

V. M. Sglavo, F. De Genua, "High reliability alumina – silicon carbide laminated composites by Spark Plasma Sintering", in "Properties and Applications of Silicon Carbide", Edited by R. Gerhardt, INTECH, Croatia, April 2011, p. 427-444.

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De Genua F., Sglavo V. M., "High Mechanical Reliability Alumina/Silicon Carbide Laminated Composites", in 18th European Conference on Fracture Fracture of Materials and Structures from Micro to Macro Scale, Berlin, D: DVM, 2010, p. 136-136. Atti di: 18th European Conference on Fracture, Fracture of Materials and 161 Structures from Micro to Macro Scale, Dresden, D, 30th August-3rd September 2010.

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Participation to Congresses

De Genua F., Sglavo V. M., "High mechanical reliability alumina-silicon carbide laminated composites", VIII Convegno nazionale sulla Scienza e Tecnologia dei Materiali (Consorzio INSTM), Aci Castello, Catania, Italy, 26th-29th June, 2011. Poster.

De Genua F., Sglavo V. M., "High mechanical reliability alumina-silicon carbide laminated composites", 12th Conference of the European Ceramic Society (ECerS XII), Stockholm, Sweden, 19th-23th June, 2011. Poster.

De Genua F., Sglavo V. M., "High strength alumina-silicon carbide laminated composites by Spark Plasma Sintering", International Conference on the Mechanical Behaviour of Materials (ICM11), Lake Como, Italy, 5th-9th June, 2011. Oral presentation.

Sglavo V. M., De Genua F., Conci A., "Influenza della temperatura di maturazione sulla struttura del cemento Sorel" 10° Convegno Nazionale AIMAT, Capo Vaticano (VV), Italy, 5th - 8th September 2010. Oral presentation.

Sglavo V. M., De Genua F., "Laminati Compositi in Allumina e Carburo di Silicio mediante Spark Plasma Sintering", 10° Convegno Nazionale AIMAT, Capo Vaticano (VV), Italy, 5th - 8th September 2010. Poster.

De Genua F., Sglavo V. M., "High Mechanical Reliability Alumina/Silicon Carbide Laminated Composites", in 18th European Conference on Fracture, Fracture of Materials and Structures from Micro to Macro Scale, Dresden, Germany, 30th August – 3rd September, 2010. Oral presentation.

V. M. Sglavo, F. De Genua, "High reliability alumina – silicon carbide laminated composites", CIMTEC 2010, Montecatini Terme, Italy, 6th -11th June, 163 2010. Oral presentation.

V. M. Sglavo, F. De Genua, A. Molinari, F. Casari, "Alumina – silicon carbide laminated composites by spark plasma sintering", ICACC33, Daytona Beach, Florida, USA, 18th -23th January, 2009. Oral presentation.

Other activities

Teaching assistant. Ceramics Engineering. University of Trento, (2010).

Teaching assistant. Ceramics Engineering. University of Trento, (2009).

Research contract. Physical and mechanical characterization of magnesium oxychloride (Sorel) cements. University of Trento, (2009).

Teaching assistant. Materials Science and Technology. University of Trento, (2008).

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